

Space Weather Impact on Global Navigation Satellite Systems

S. Skone

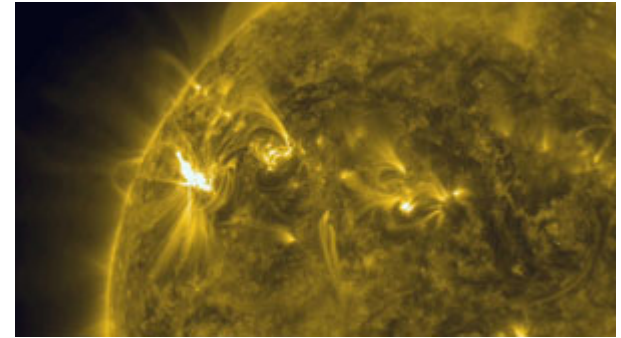
*Department of Geomatics Engineering
Schulich School of Engineering*

Solar storm could affect power grids, GPS

The Associated Press

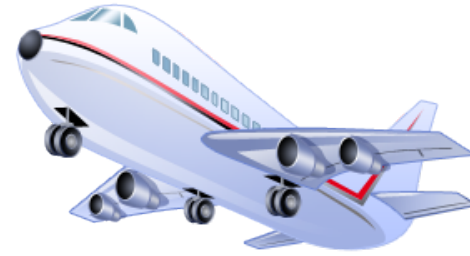
Posted: Mar 7, 2012 12:08 PM ET

Last Updated: Mar 7, 2012 2:05 PM ET



“The largest solar storm in five years is racing toward Earth, threatening to unleash a torrent of charged particles that could disrupt power grids, **GPS** and airplane flights.”

Which GPS/GNSS users are affected?

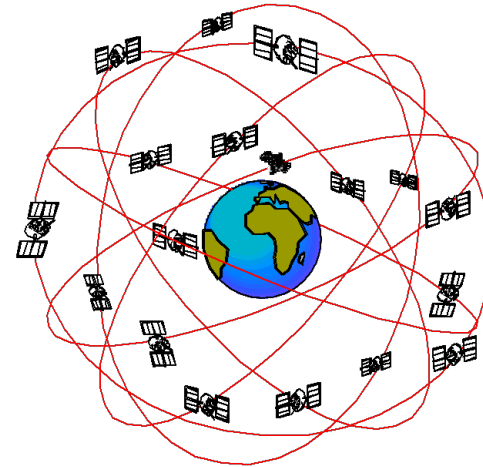


?



Global Navigation Satellite System: GPS

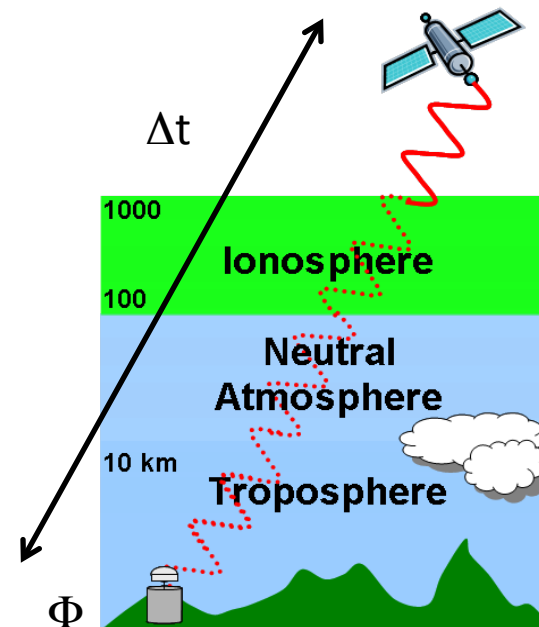
- Nominally 24 satellites orbiting 20,000 km above the Earth
- 6 orbital planes
- Transmits on multiple UHF frequencies
- Passive system
- Coarse positioning and precise positioning applications



Observations

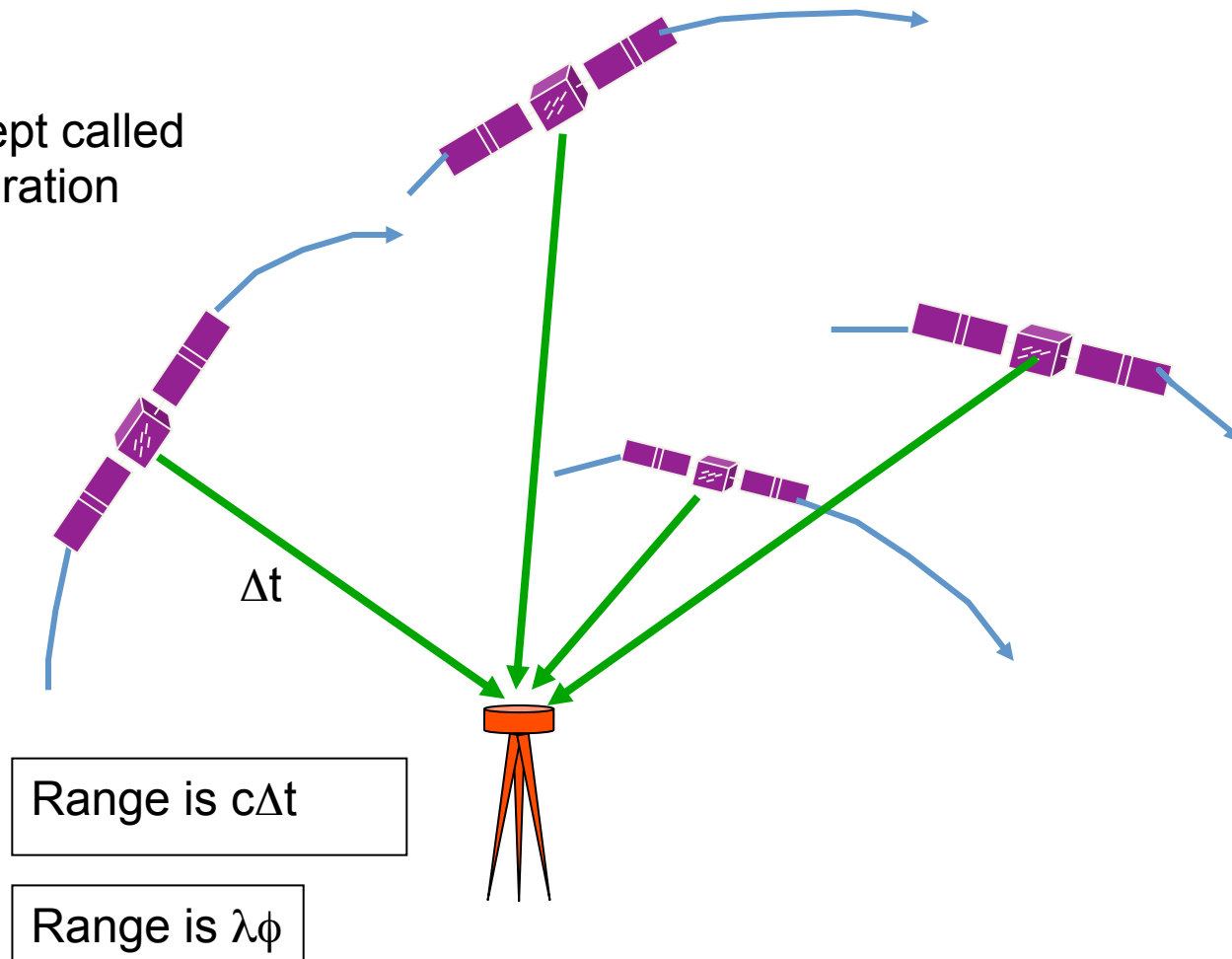
Pseudorange (1-3 m accuracy)

Carrier phase (cm-level accuracy)

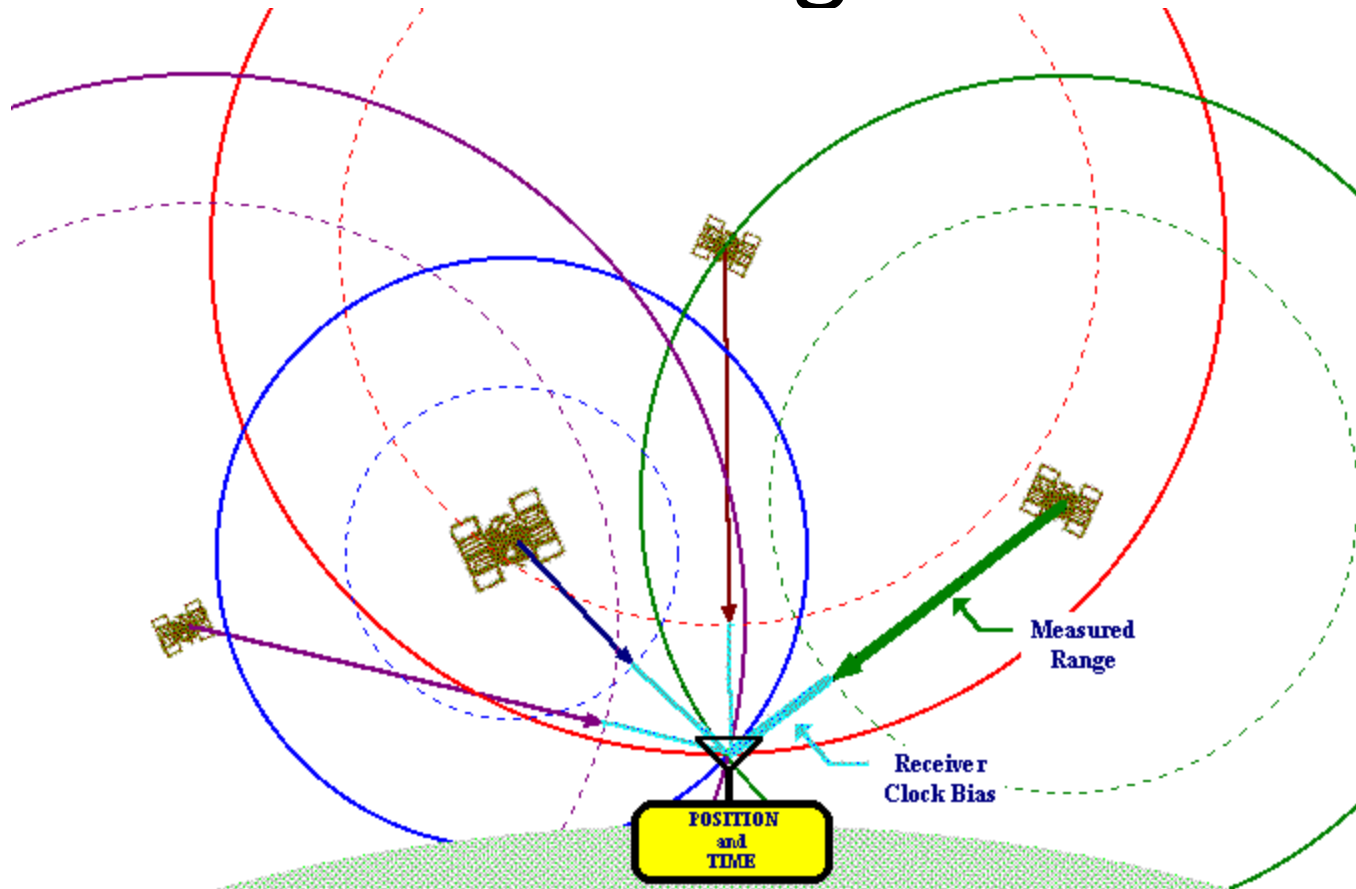


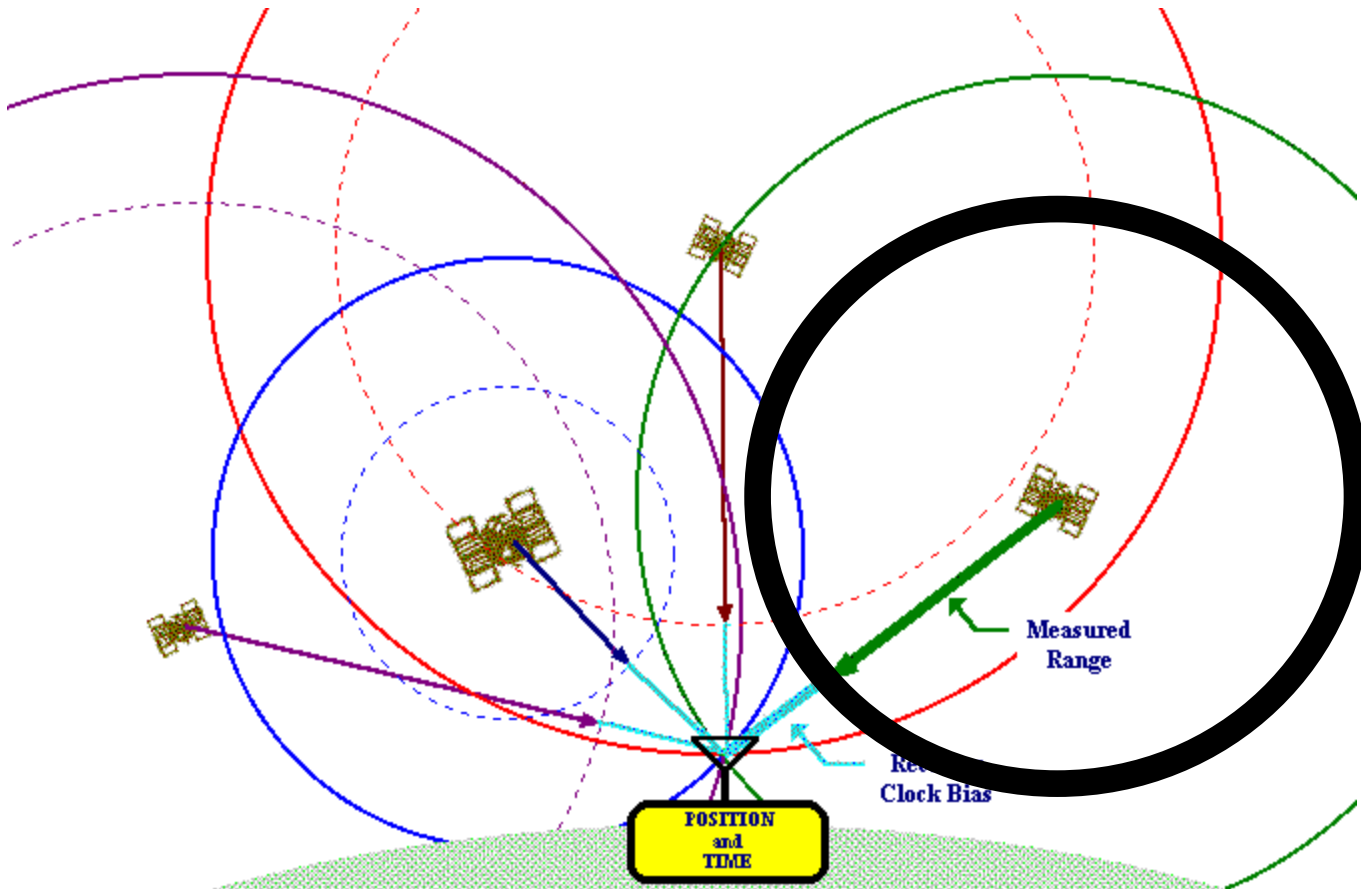
How does GPS work?

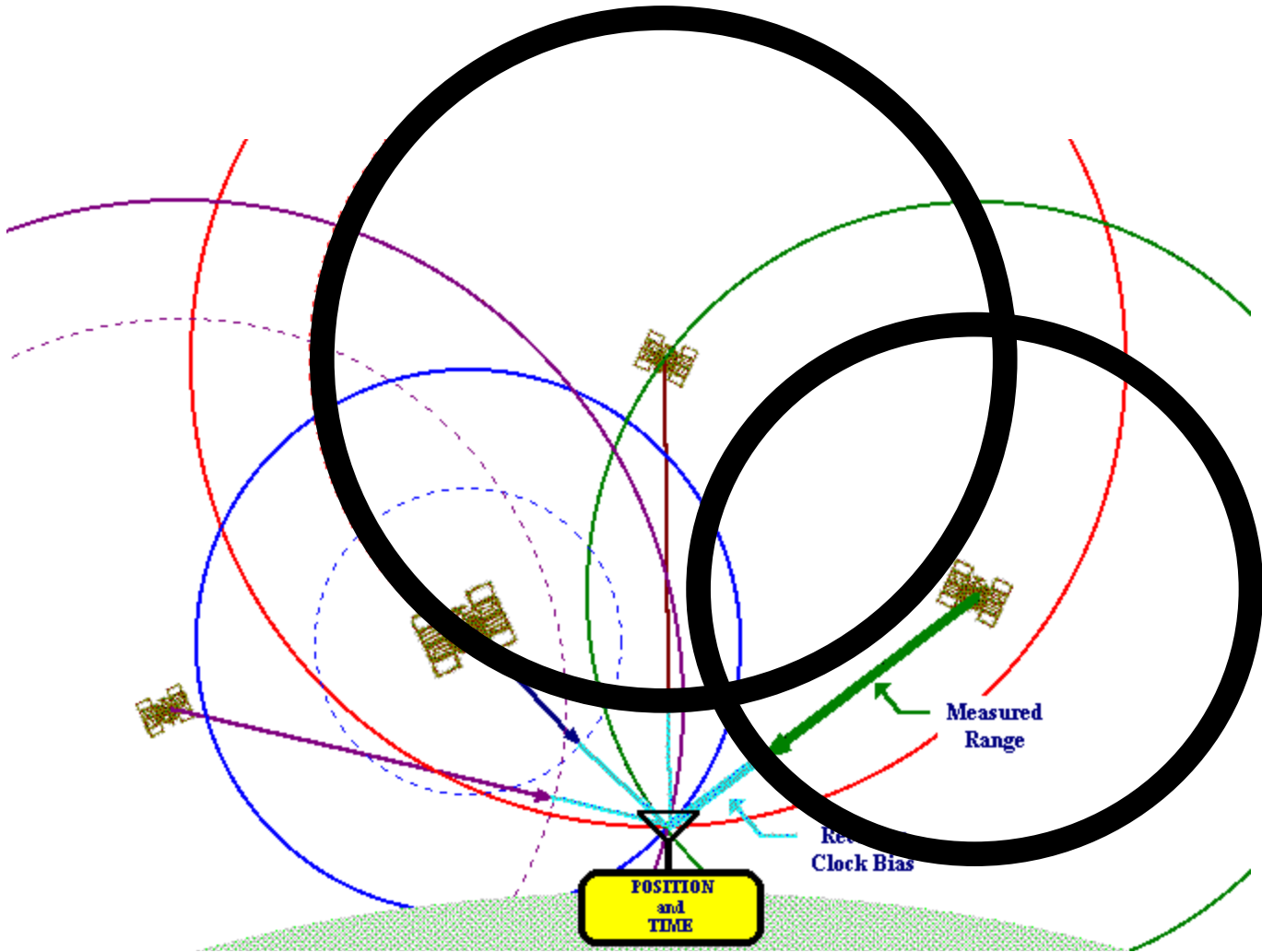
Concept called
Trilateration

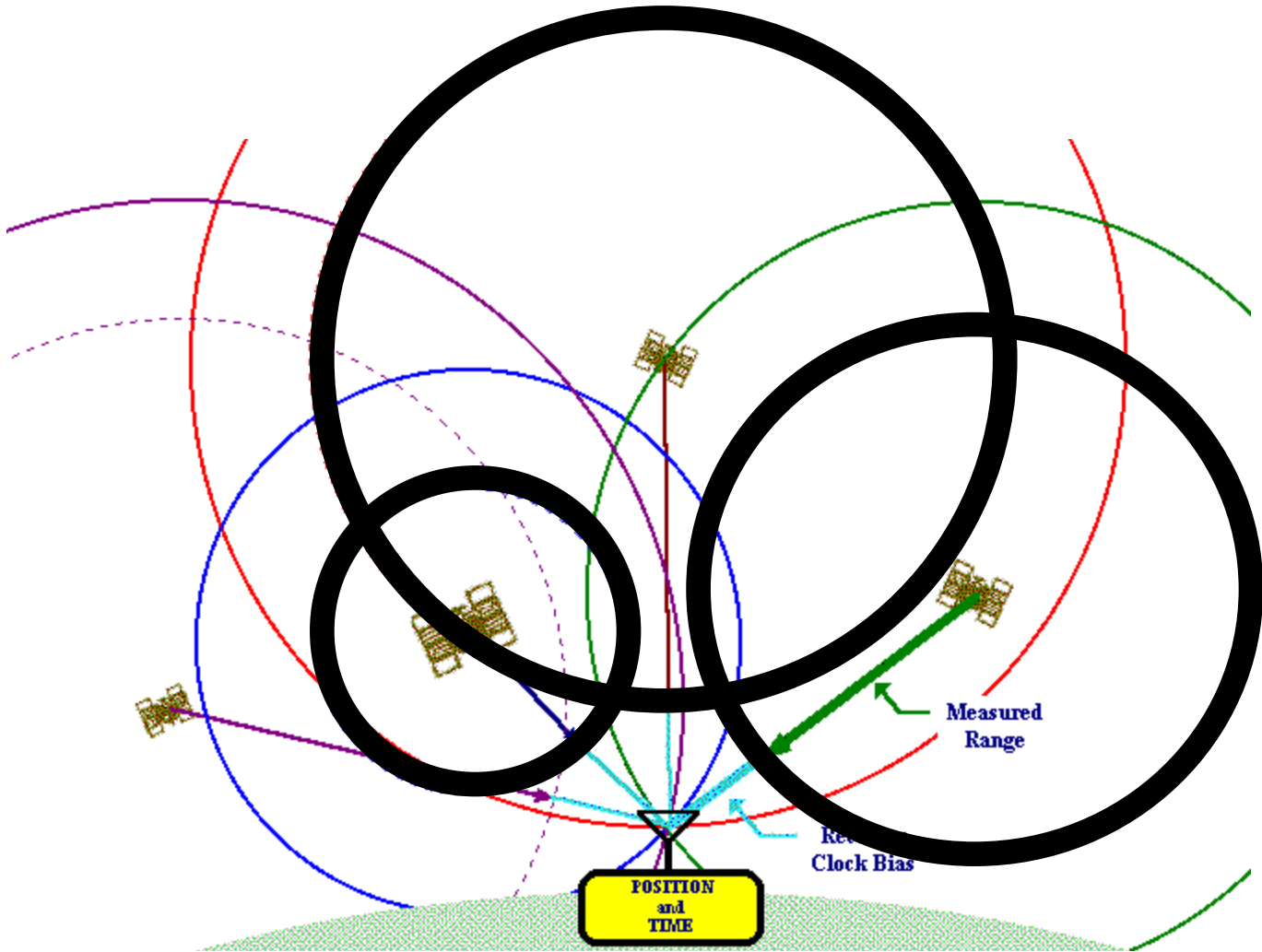


GPS Positioning Solution

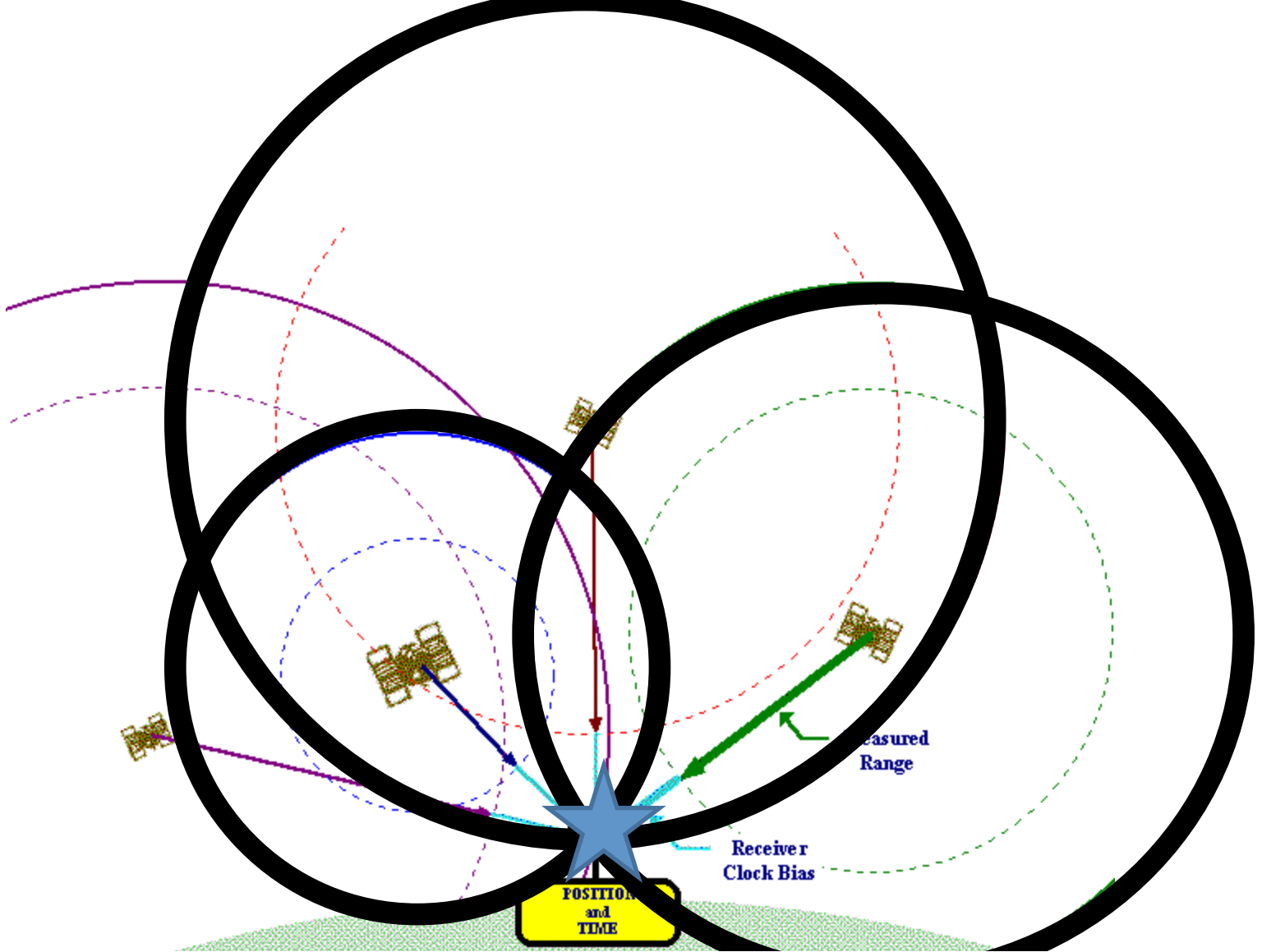






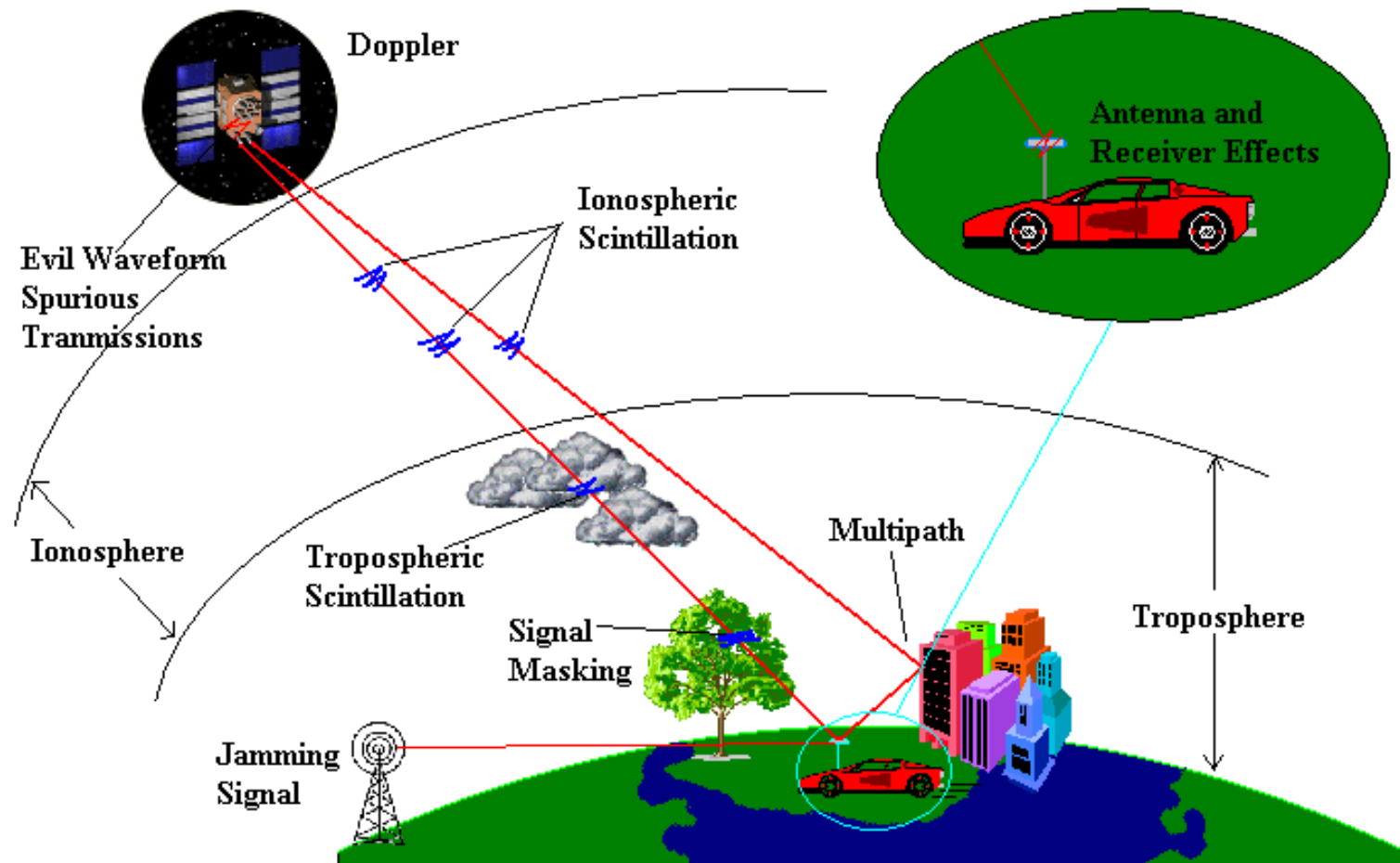


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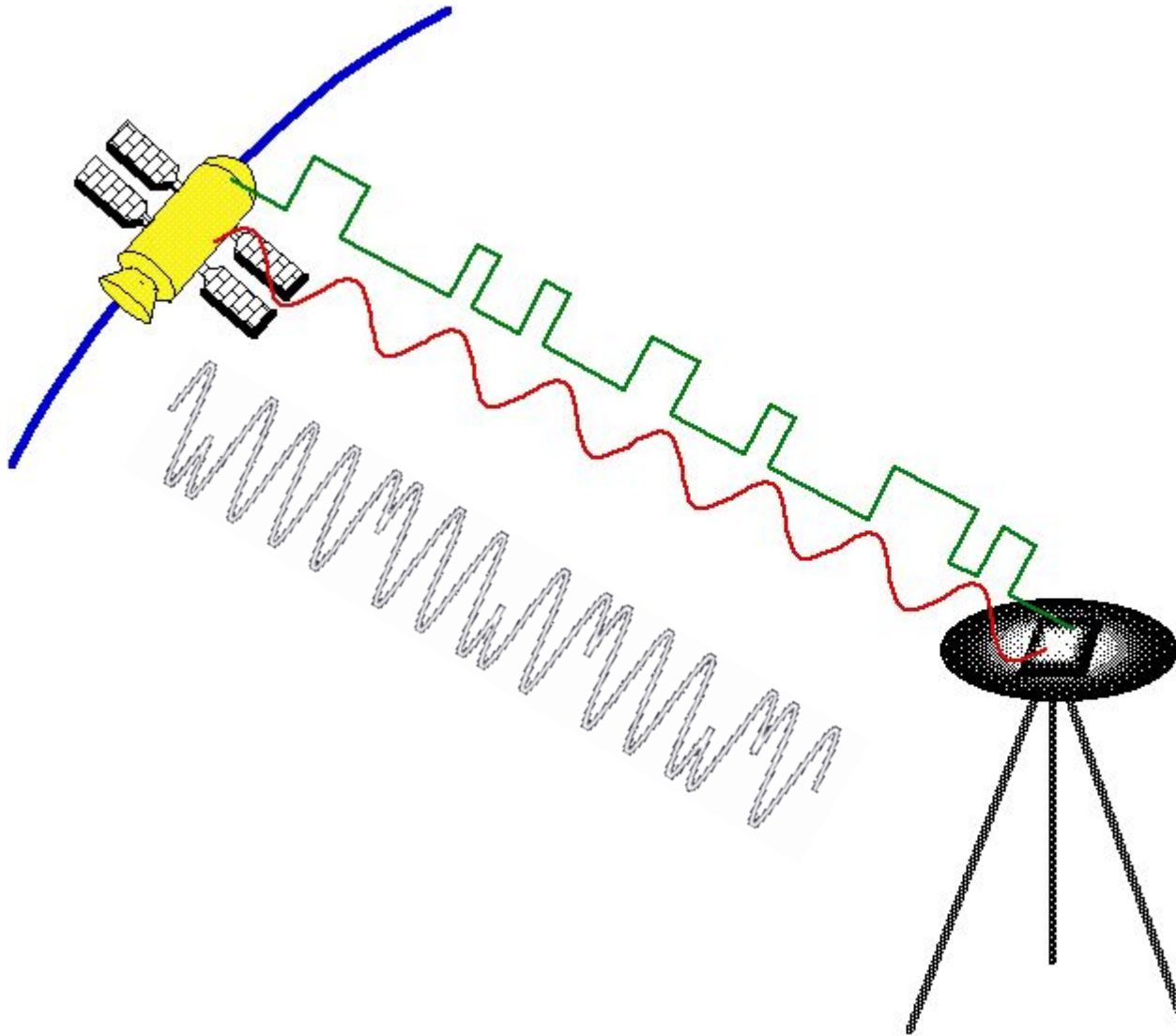


RF Signal Deterioration and Range Error

Orbit Error ($\Delta x, \Delta y, \Delta z$)



GPS Observations

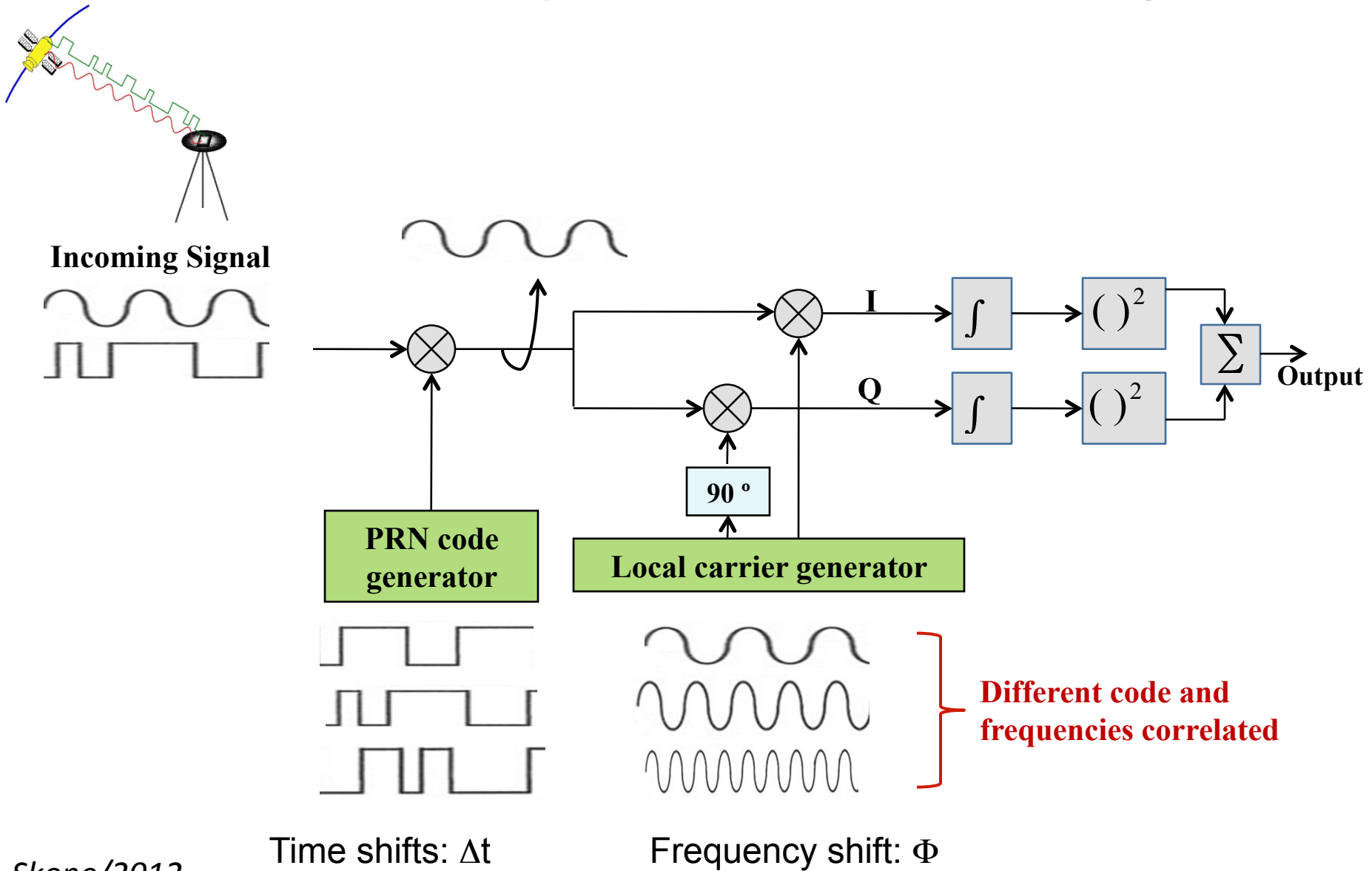


Receiver Observations

Travel time: Δt

Phase: Φ

Receiver Acquisition and Tracking



GPS Positioning Accuracy



Low

(single frequency,
metre-level accuracy)

High

(multiple frequencies,
centimetre-level accuracy)

Ionosphere Index of Refraction

$$n_p^2 = 1 - \frac{X}{1 - iZ - \frac{Y_T^2}{2(1 - X - iZ)} \pm \left[\frac{Y_T^4}{4(1 - X - iZ)} + Y_L^2 \right]^{\frac{1}{2}}}$$

(Appleton-Hartree formula)

$$X = \frac{Ne^2}{\epsilon_0 m \omega^2} = \frac{\omega_p^2}{\omega^2} \longrightarrow \text{Plasma frequency}$$

$$Y_L = \frac{eB_L}{m\omega} = \frac{\omega_L}{\omega} \longrightarrow \text{Gyrofrequency}$$

$$Y_T = \frac{eB_T}{m\omega} = \frac{\omega_T}{\omega} \longrightarrow \text{Gyrofrequency}$$

$$Z = \frac{\nu}{\omega} \longrightarrow \text{Collision frequency}$$

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Range error?

For GPS, we assume $v_g = c$, $v_p = c$ and to derive range and phase observations

$$\lambda = \frac{\lambda_0}{n_p} = \lambda_0$$

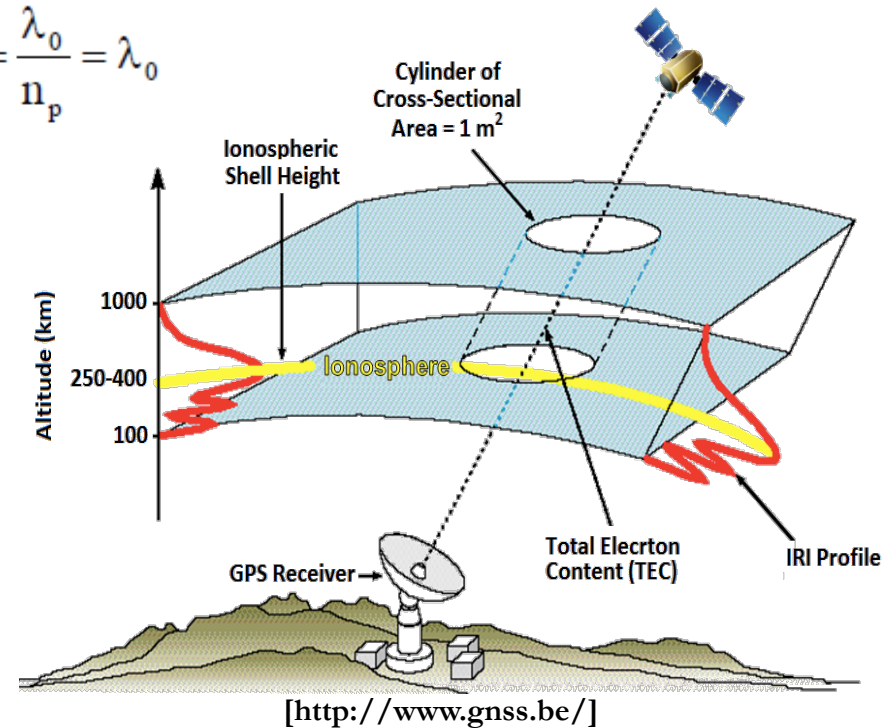
This is not correct \Rightarrow range error

i.e

$$|\Delta v_p| = |\Delta v_g| = \Delta v$$

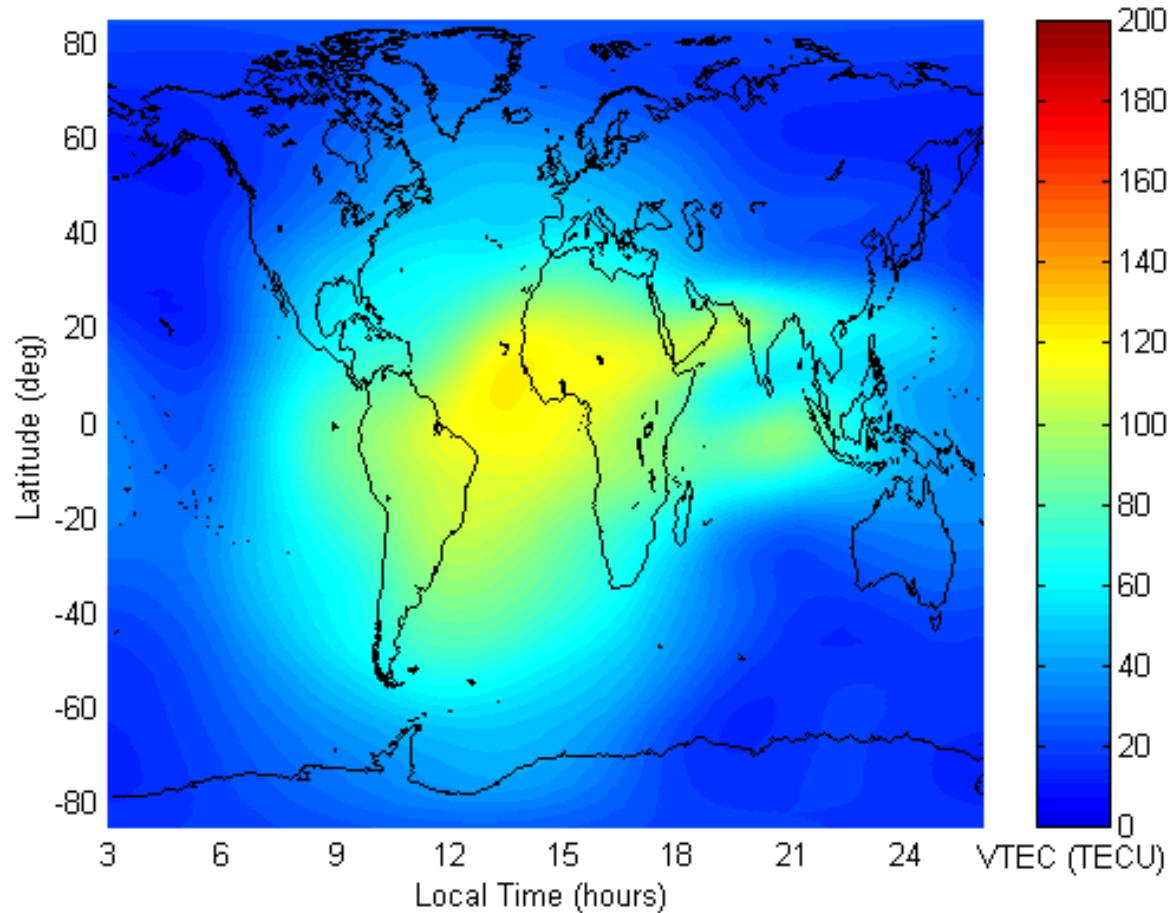
$$\Delta R = \int \Delta v dt = \frac{c}{2\omega^2} \int_{\text{travel time}} \omega_p^2 dt$$

$$\Delta R = \frac{40.3}{f^2} TEC$$



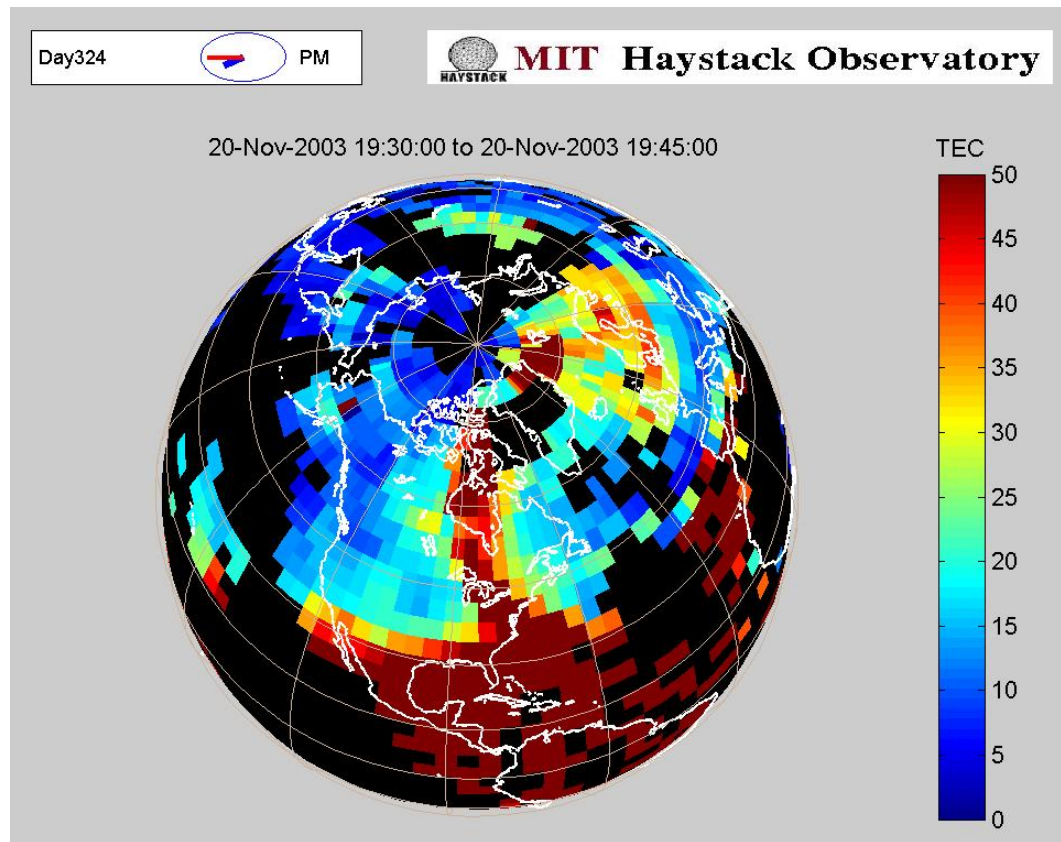
Spatial Distribution of VTEC during Solar Maximum (Equinox)

March 2000



Space Weather Event: Storm Enhanced Density

VTEC



**How would you reduce ionospheric
range error for GPS?**

Use an Expensive Dual Frequency GPS Receiver

Calculating TEC (Dual Frequency)

- Assume measurements on two frequencies f_1, f_2 (i.e. GPS)
- Different range errors:

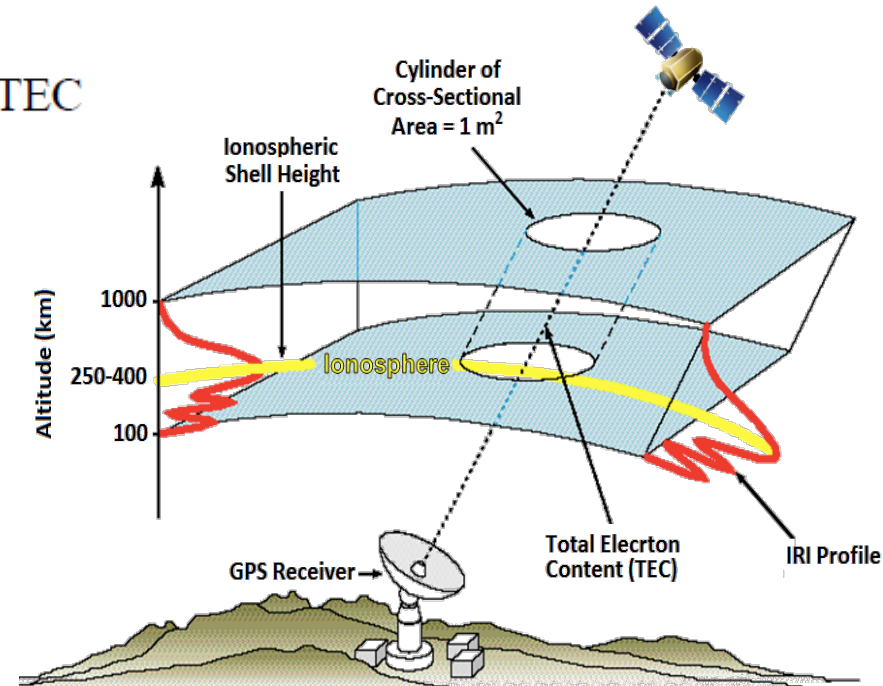
$$\Delta R_1 = \frac{40.3}{f_1^2} \text{TEC} \quad \Delta R_2 = \frac{40.3}{f_2^2} \text{TEC}$$

- We can compute TEC:

$$R_1 - R_2 = \Delta R_1 - \Delta R_2 = 40.3 \left(\frac{1}{f_1^2} - \frac{1}{f_2^2} \right) \text{TEC}$$

$$\text{TEC} = \frac{1}{40.3} \left(\frac{f_1^2 f_2^2}{f_2^2 - f_1^2} \right) (\Delta R_1 - \Delta R_2)$$

L1 = 1.5 GHz
L2 = 1.2 GHz



[<http://www.gnss.be/>]



S. Skone/2012

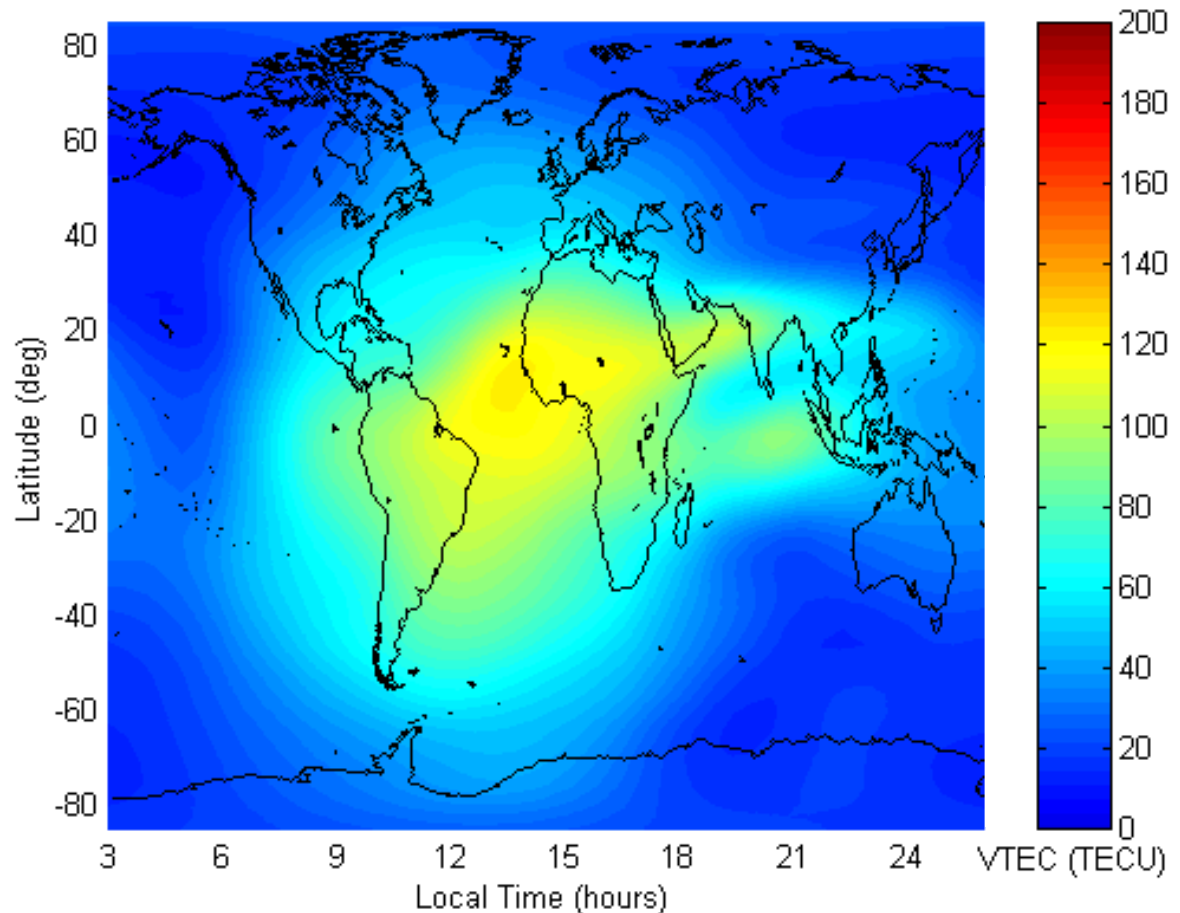
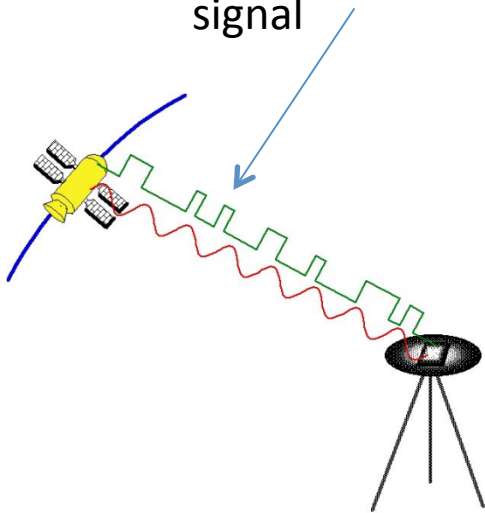
How would you model ionospheric range error for a low-cost user?

Single frequency only!



Eight values used to represent the global ionosphere. These values are broadcast to GPS users.

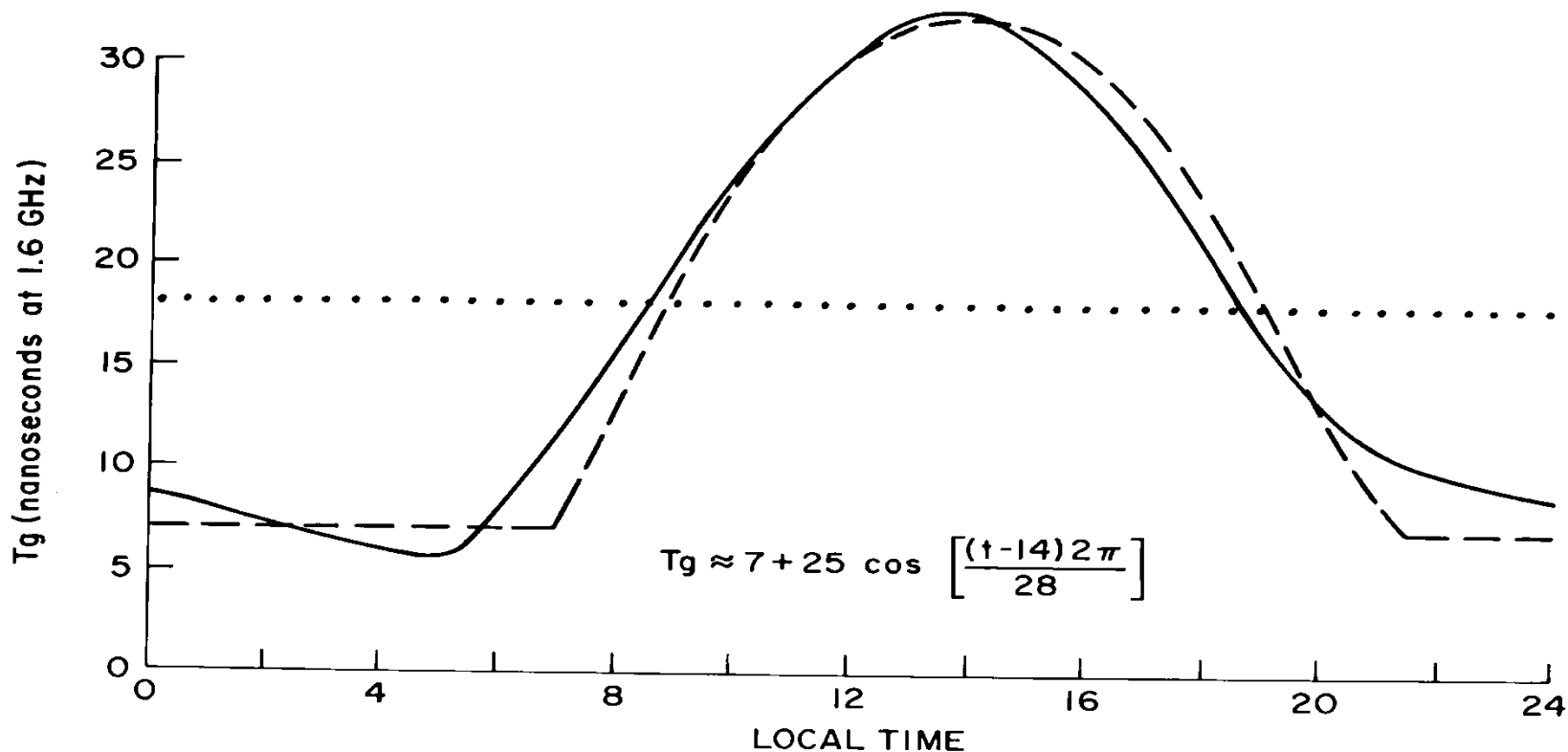
Information encoded on signal



Broadcast (Klobuchar) Ionospheric Correction Algorithm

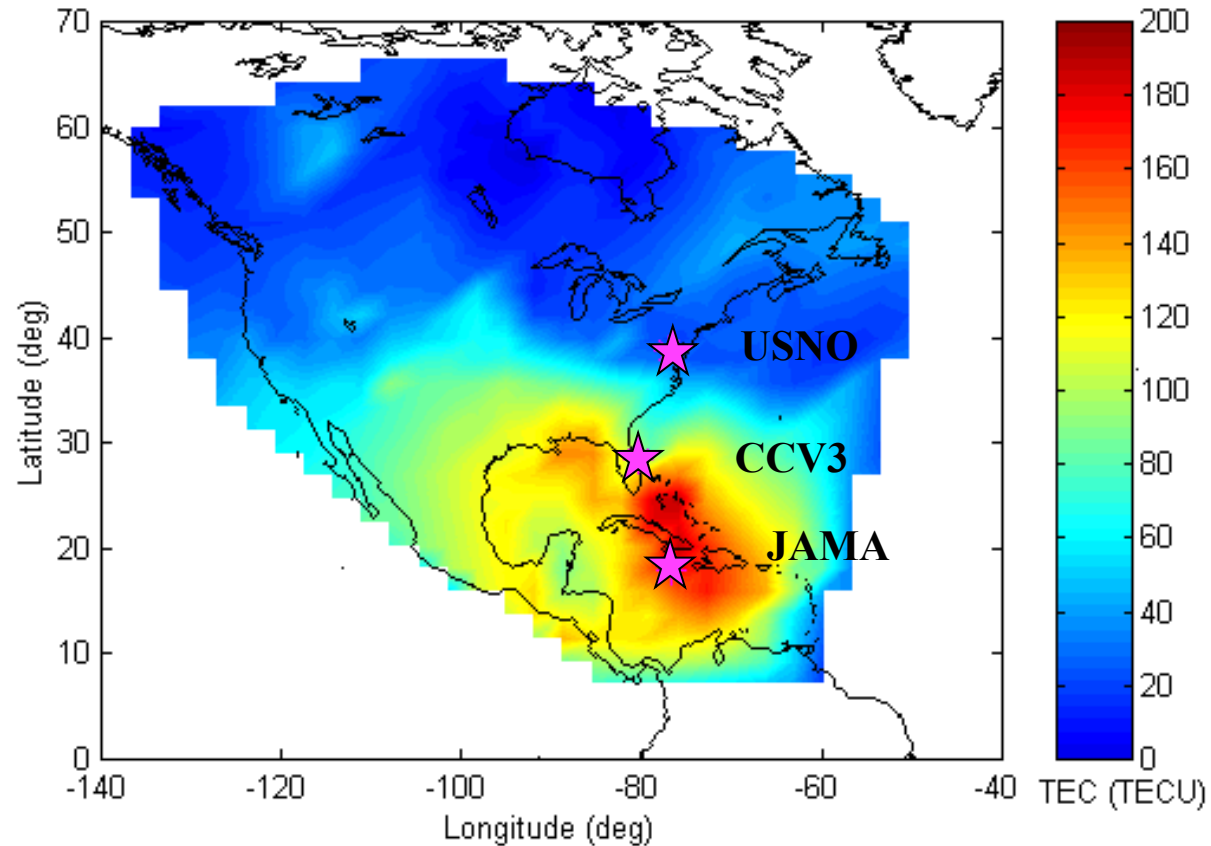
JAMAICA, WEST INDIES
SEPTEMBER 1970

— ACTUAL DATA. T_g rms = 19.5 (NO CORRECTION)
..... CONSTANT FIT. ΔT_g rms = 9.4 (52% CORRECTION)
- - - COSINE FIT. ΔT_g rms = 1.94 (90% CORRECTION)



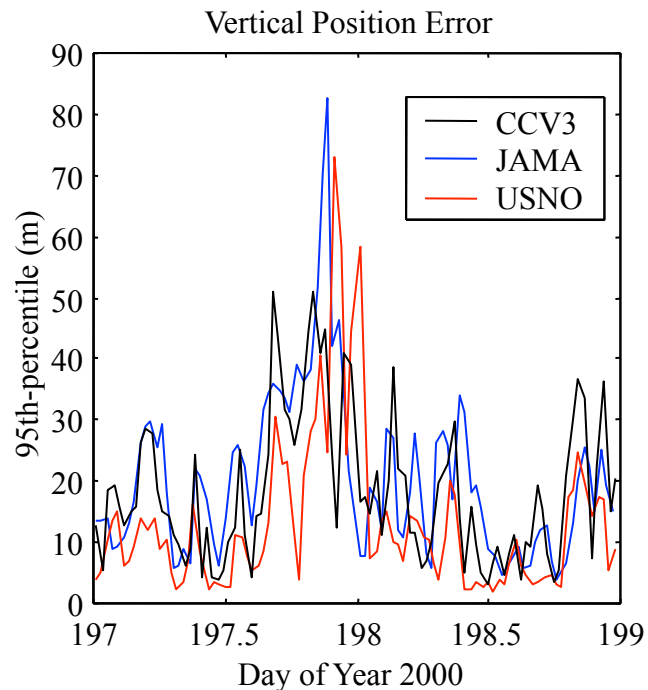
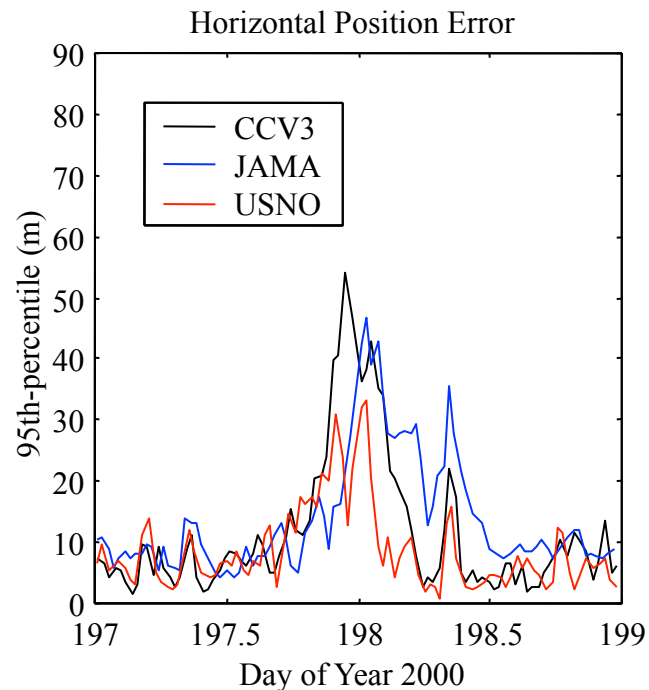
But what happens in this case?!

TEC Map July 15, 2000: 22:25 UT

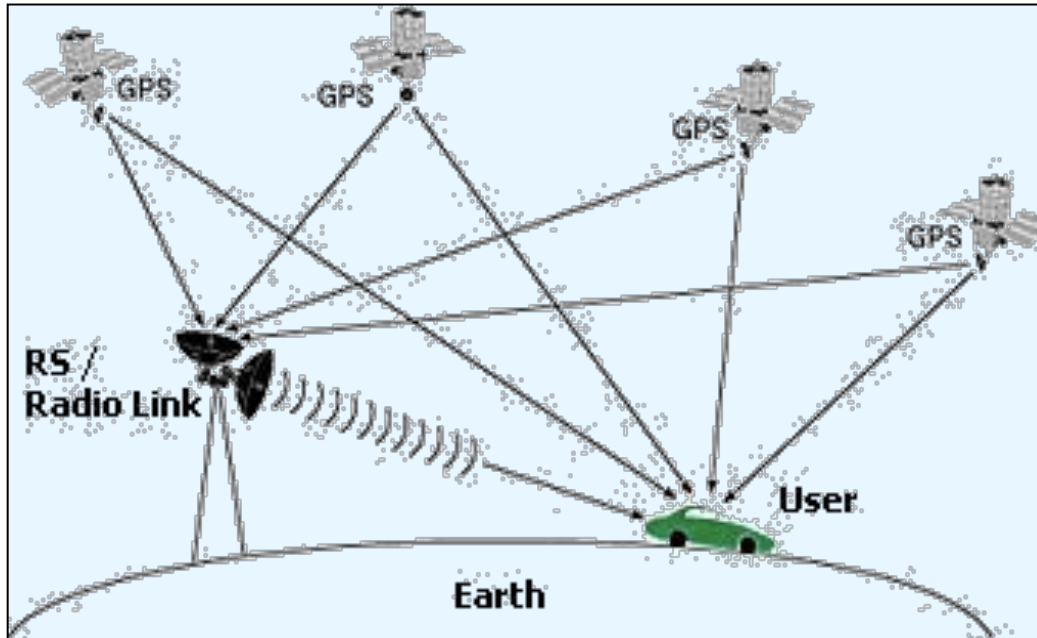


Severe storm event – not the “normal” cosine trend

Single Point Positioning Accuracies (Single Frequency)



Differential GPS



- Range corrections measured at reference station and sent to remote users
- Without DGPS... your accuracy is 5-10 metres
- With DGPS...your accuracy improves to 0.5 - 2 metres
- Accuracy degrades with baseline distance

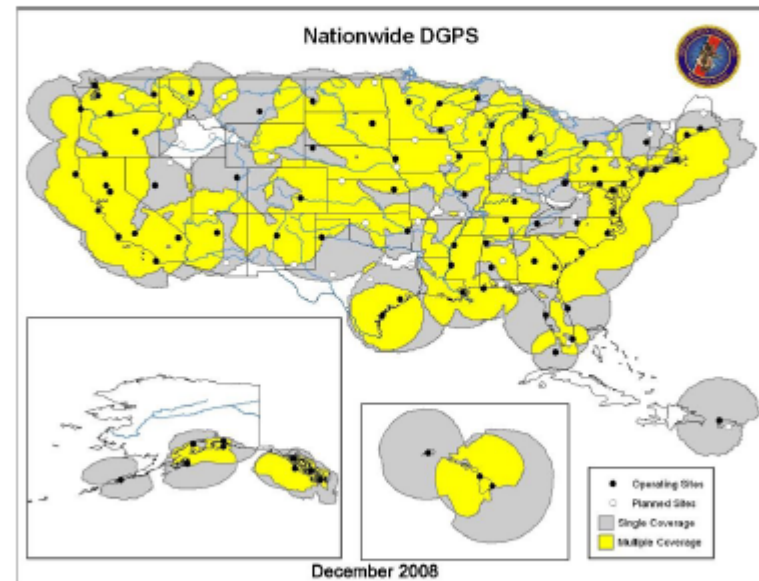
DGPS Services are common in many countries

East Coast DGPS Coverage

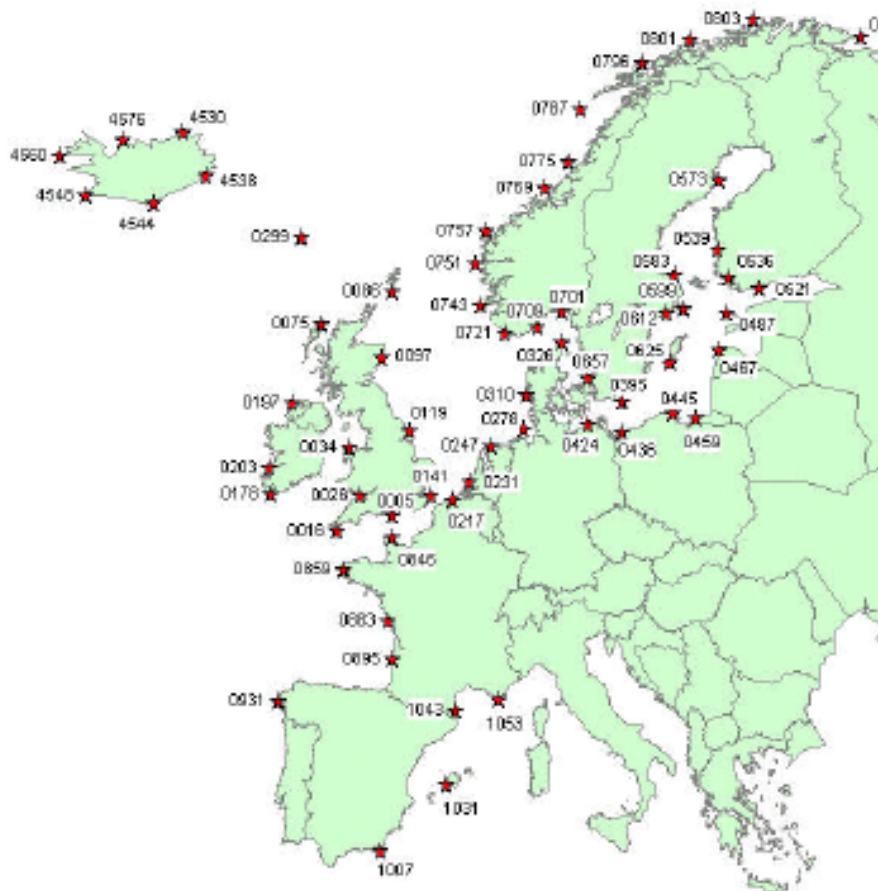


Canada

- The United States DGPS service is operated by the United States Coast Guard and has many applications in mapping and surveying, natural resource exploration/exploitation, agriculture, GIS, land-based transportation and emergency response.



<http://www.navcen.uscg.gov/dgps/coverage/CurrentCoverage.htm>

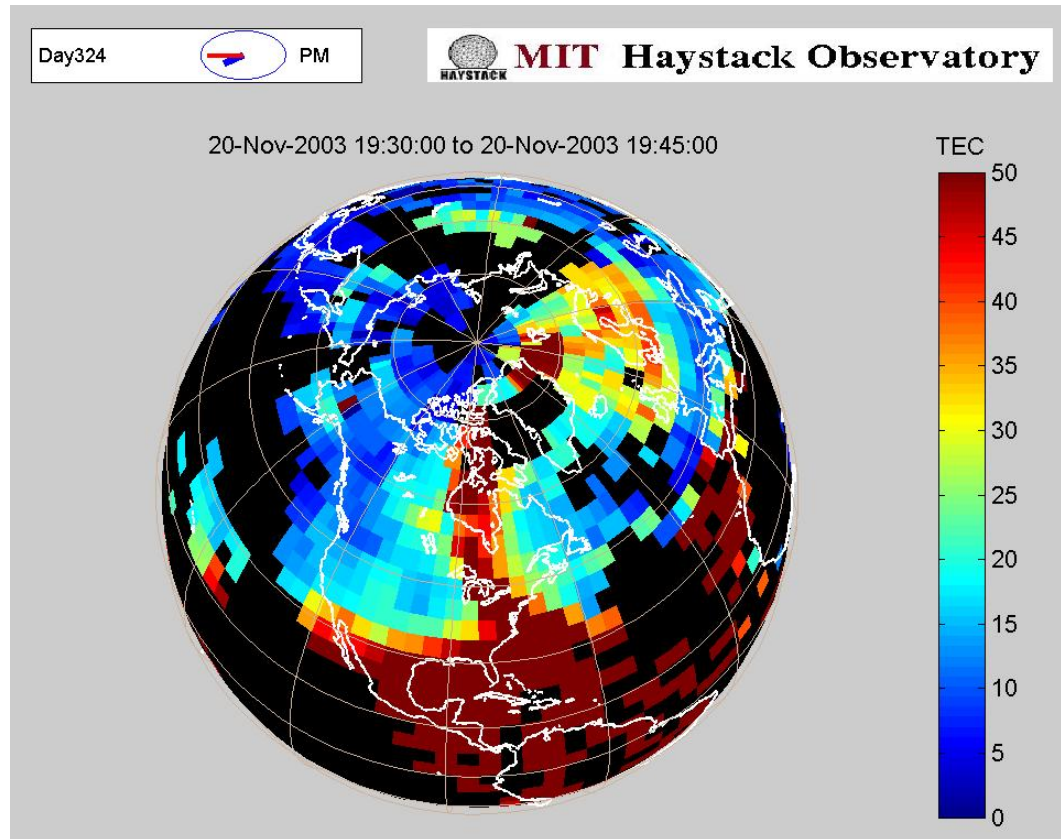


<http://www.effective-solutions.co.uk/beacons.html>

- A European public system is operated by consortium of countries. Accuracies of 10 m 2DRMS (95%) are guaranteed at ranges of 500 km.

But what happens in this case?!

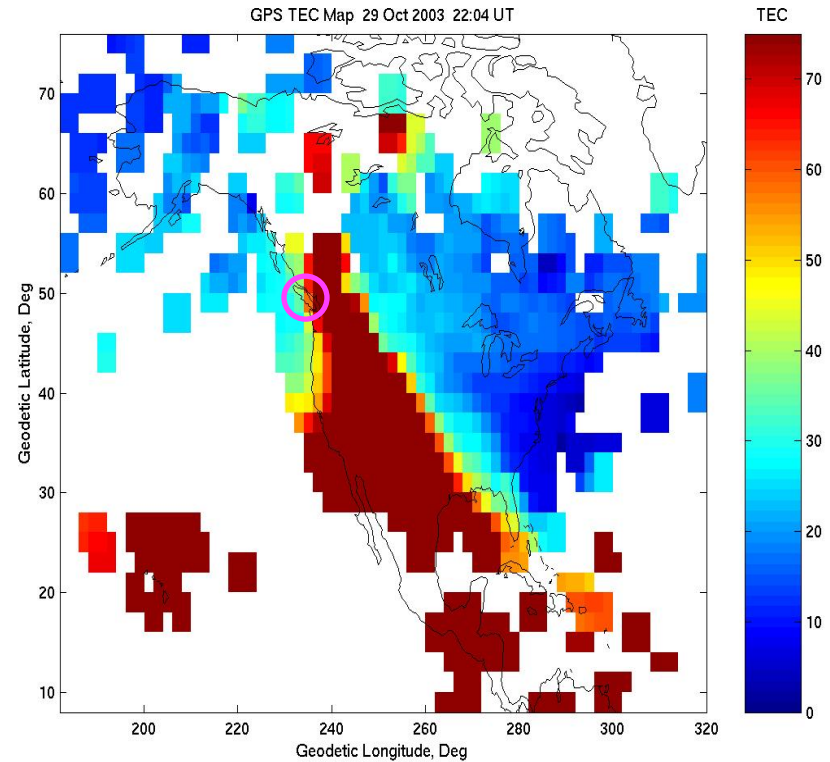
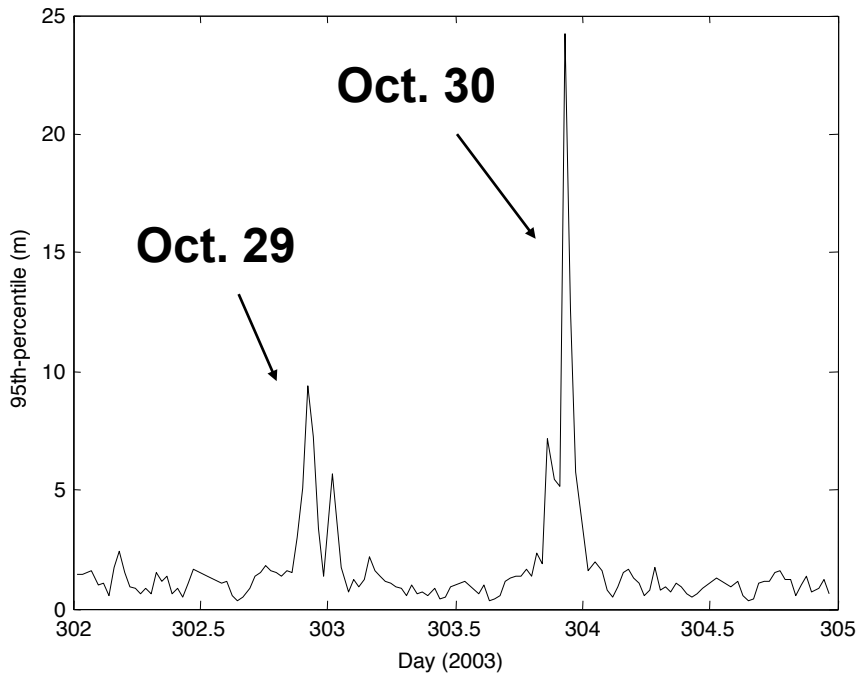
Storm Enhanced Density



Large ionosphere gradients

Example SED - October 29-31, 2003

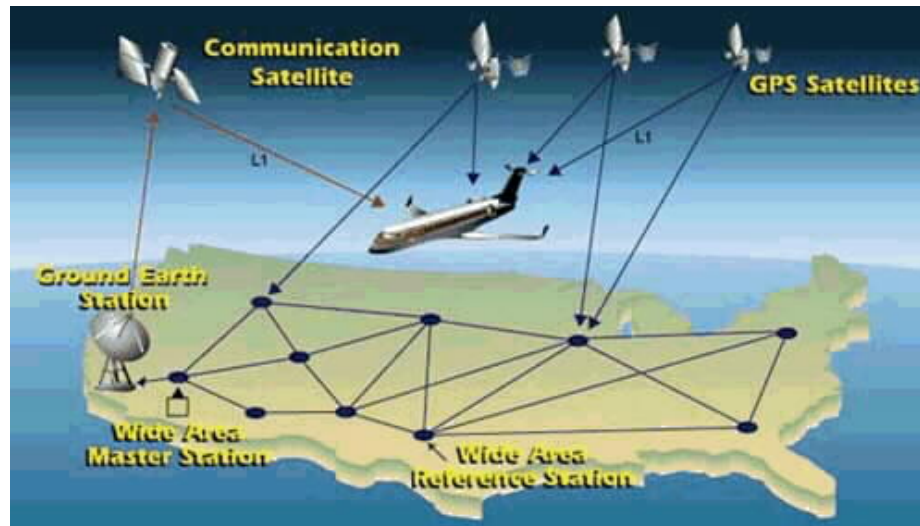
Horizontal DGPS Pos. Accuracies: 125 km Baseline



- Position accuracies > 10 m (95%) for 90 minutes

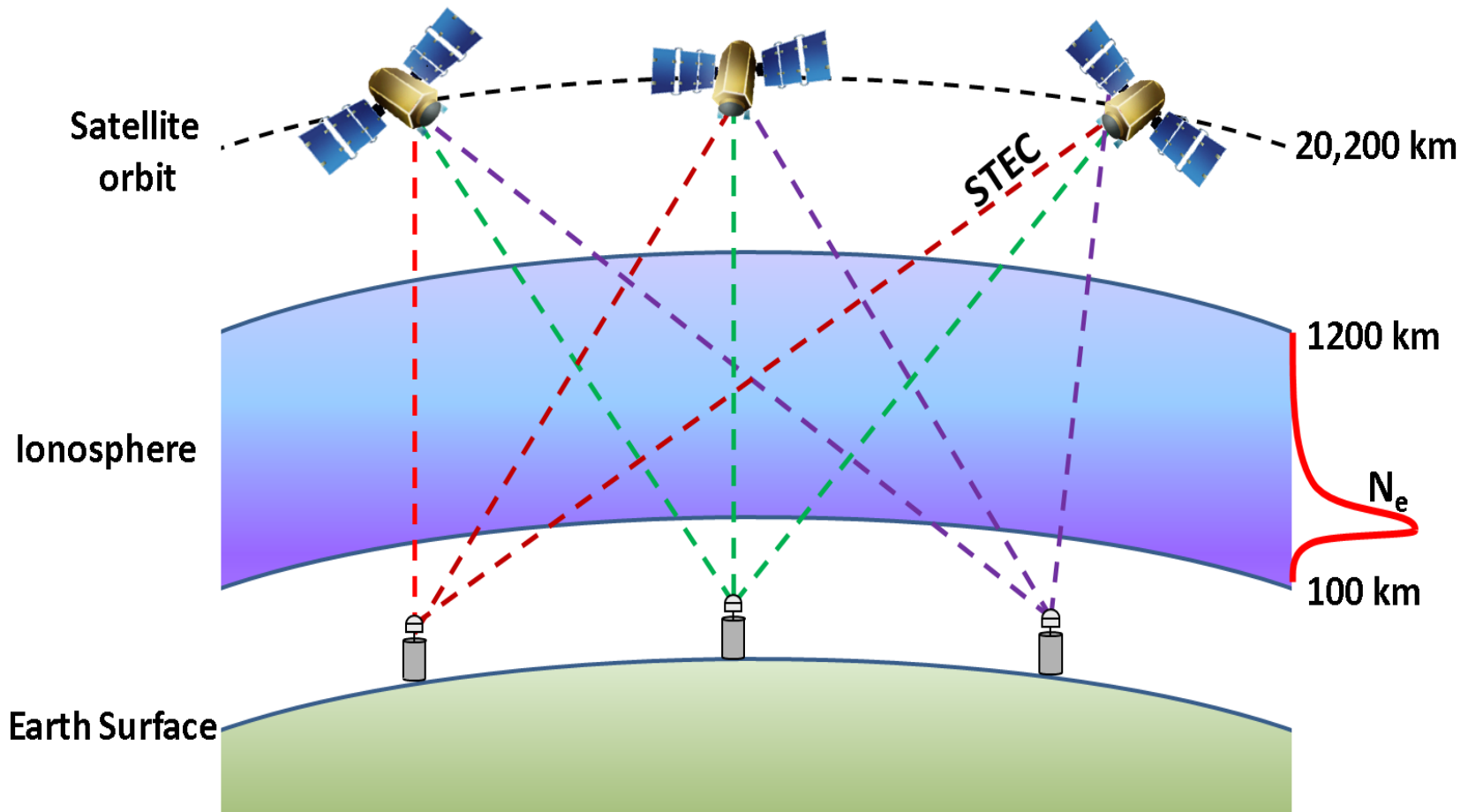


Wide Area Augmentation System

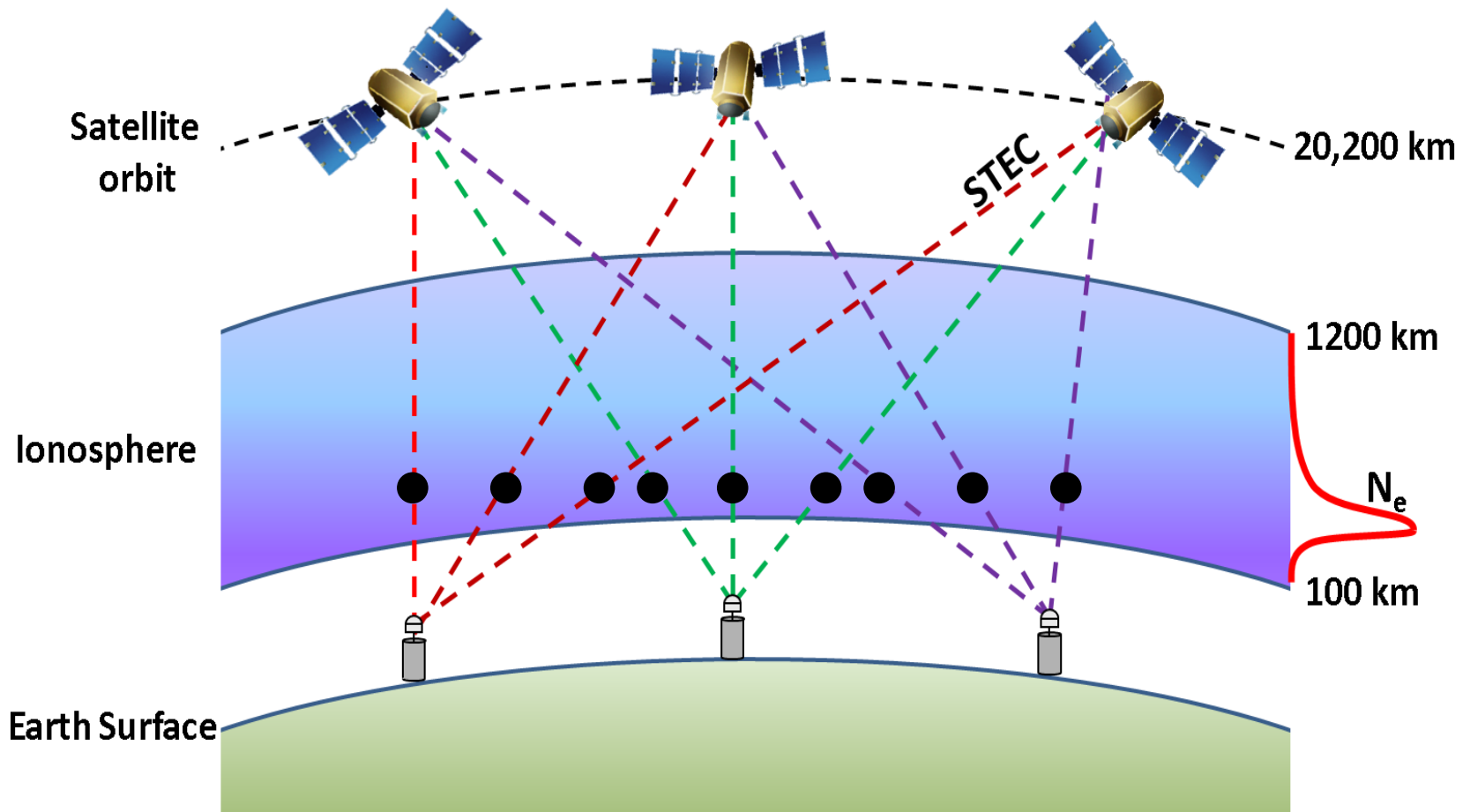


- Designed to provide reliable positioning accuracies better than 8 m (vertically and horizontally) for aircraft navigation
- 38 reference stations and 2 master stations
- WAAS vector corrections: satellite clock & orbit, and ionosphere
- WAAS messages provided by geostationary downlink
- WAAS positioning capabilities in low-cost receivers (marine and land applications)

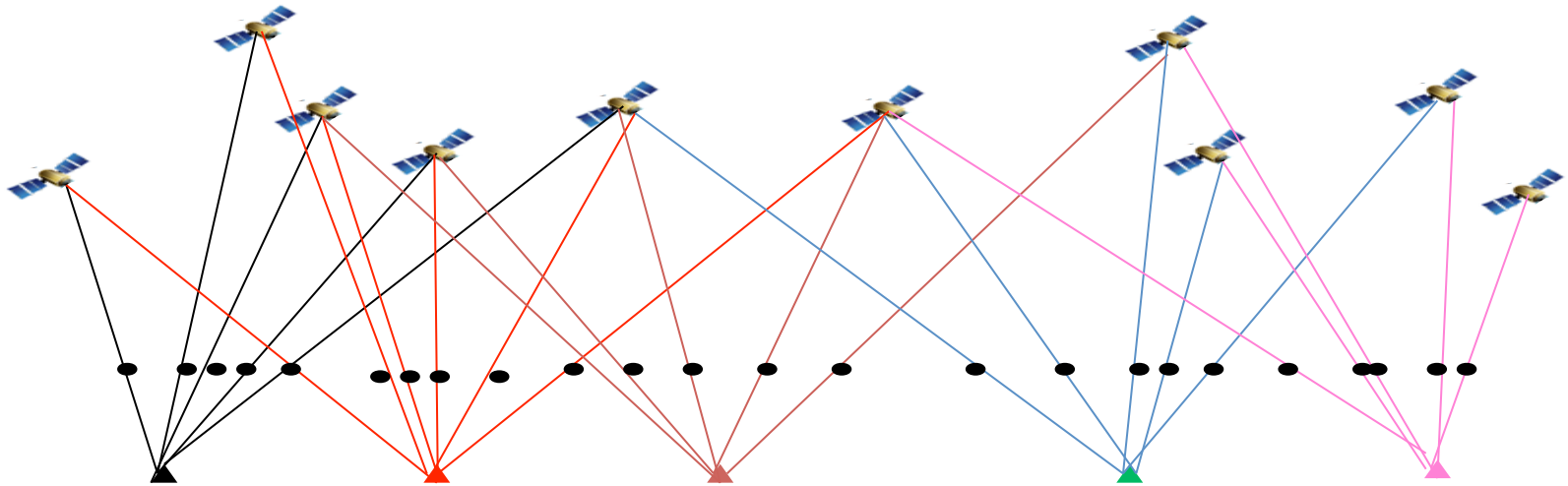
Wide Area Ionosphere Observation



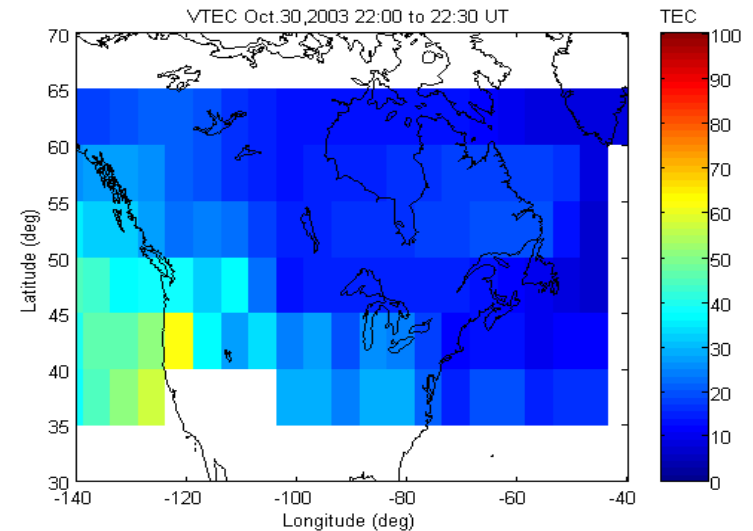
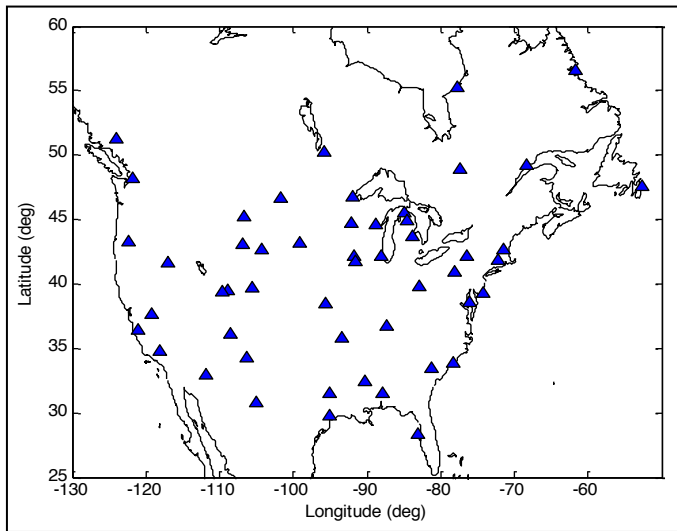
Mapped to Two Dimensions



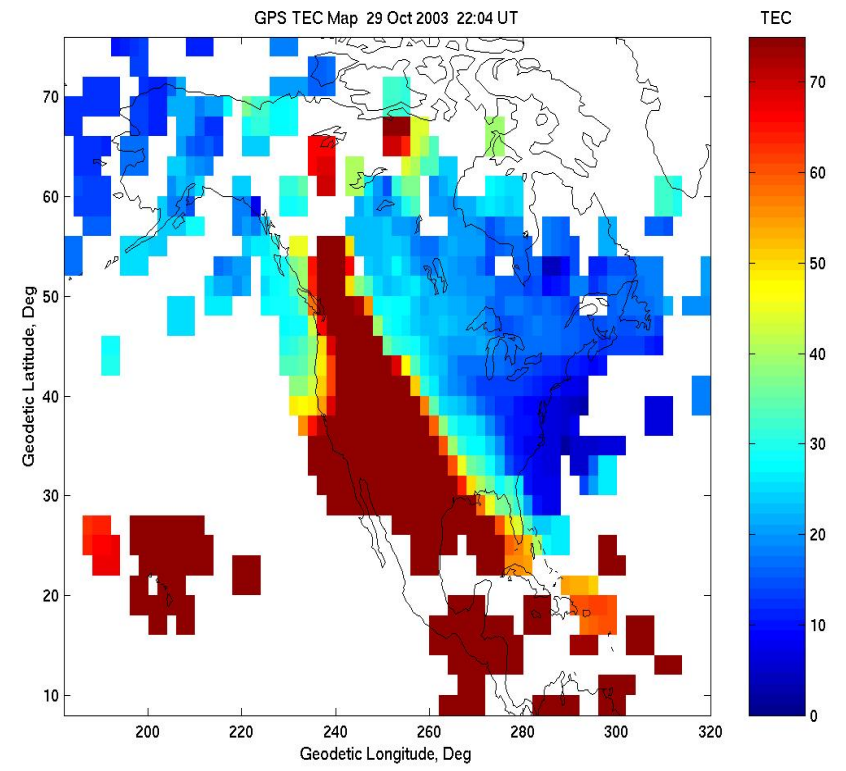
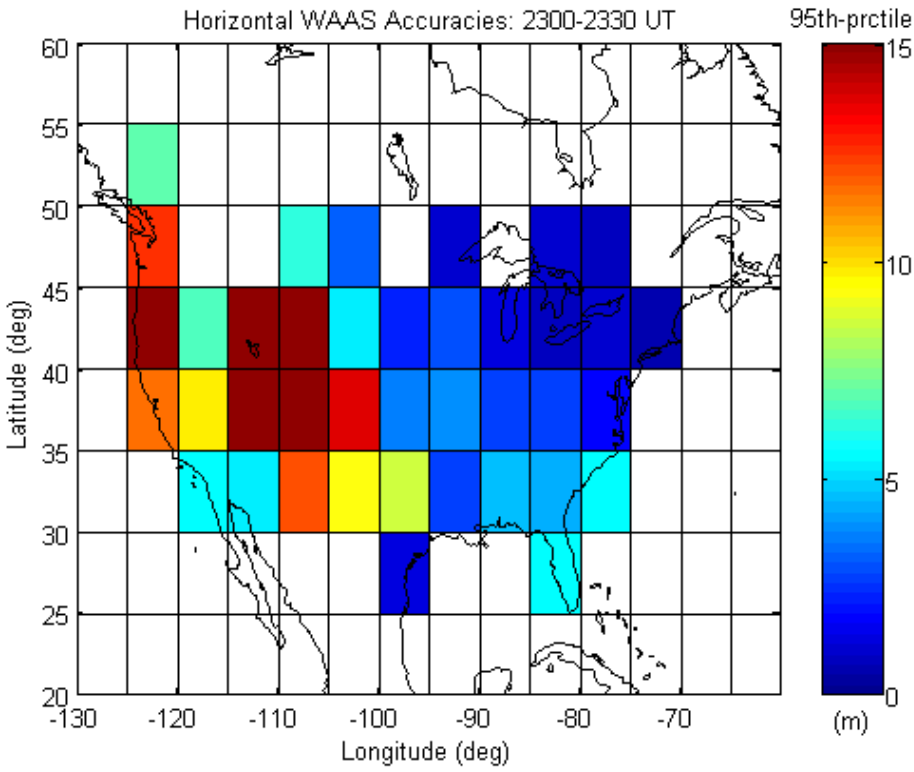
Network Observations and Output



$$F = a_0 + a_1 \Delta \lambda + a_2 \Delta \phi$$



WAAS Position Error



- Errors of >15 m horizontal

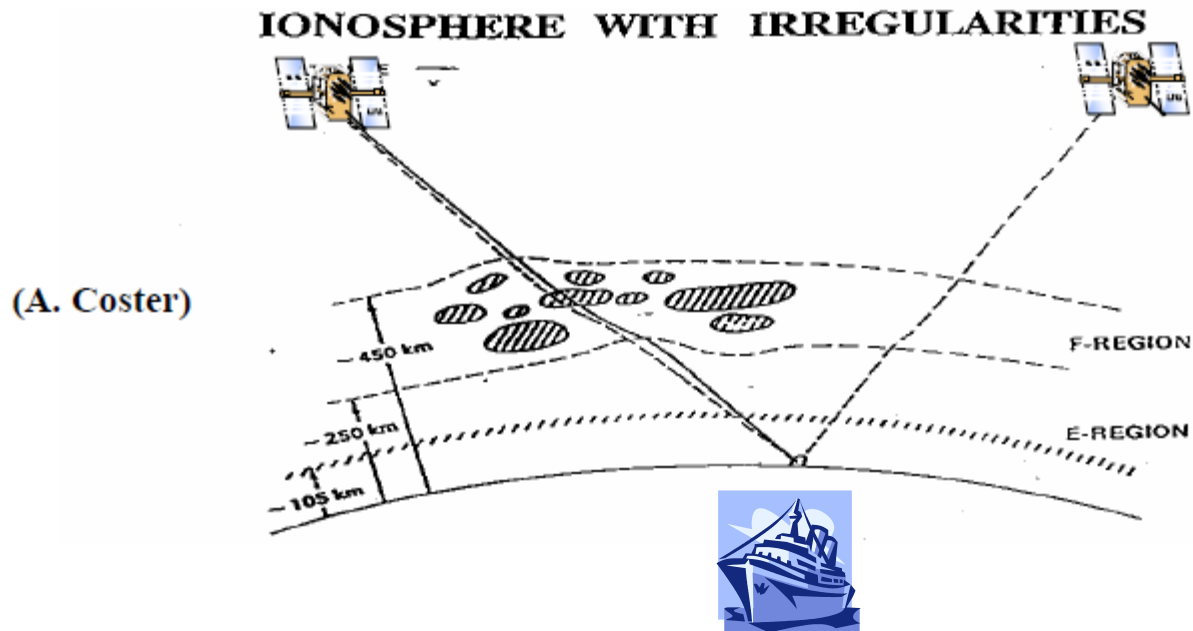


Another Effect

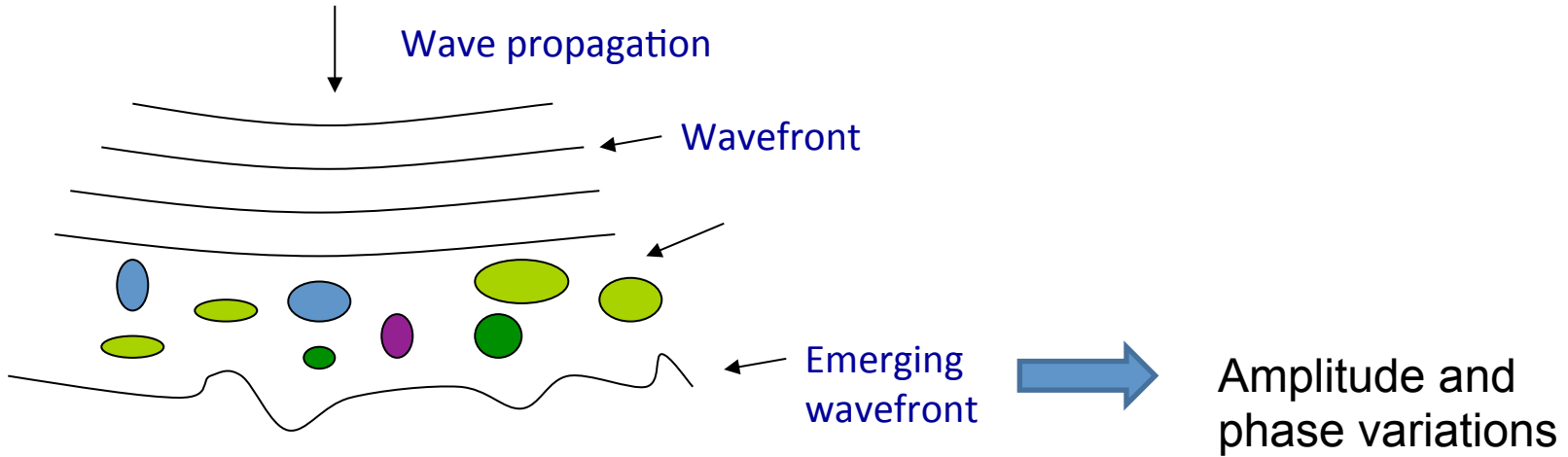
Space Weather Causes Ionospheric
Scintillation

Ionospheric Scintillation

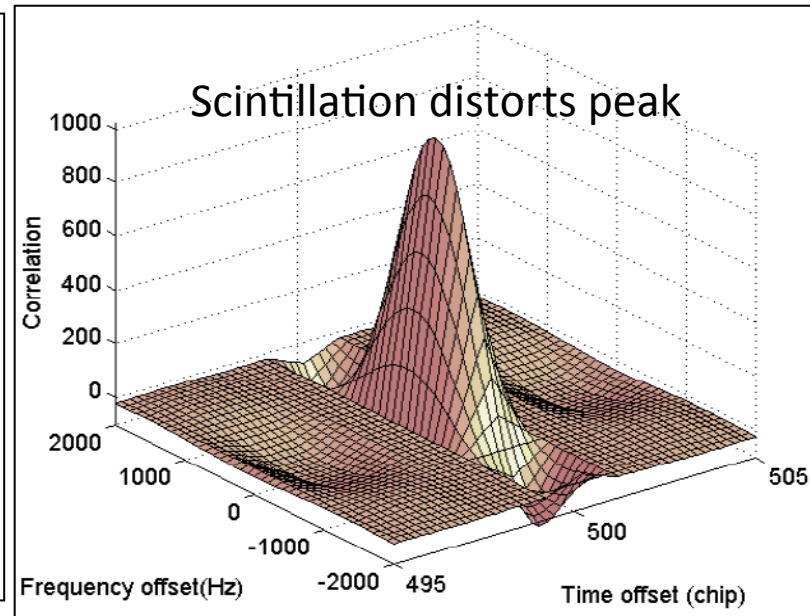
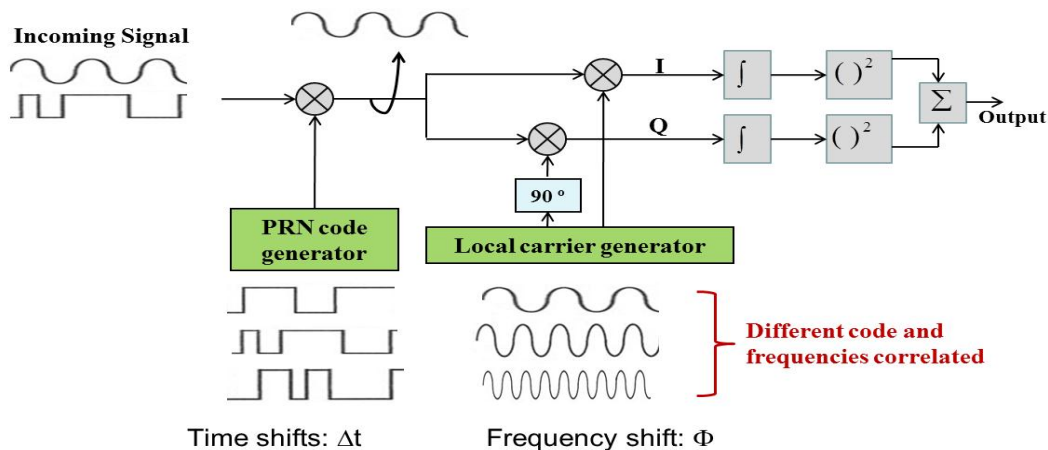
- Random rapid functions of the signal (signal strength, phase, range) about a mean value
- Phase and amplitude scintillations due to “turbulence” or irregularities (m→km in scale size) in electron density along signal path



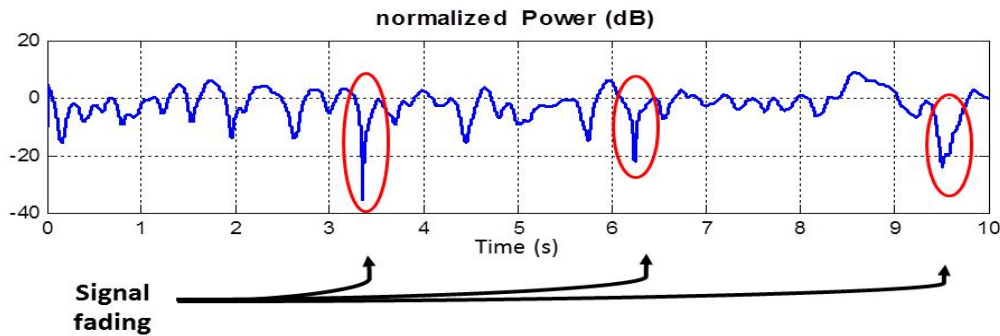
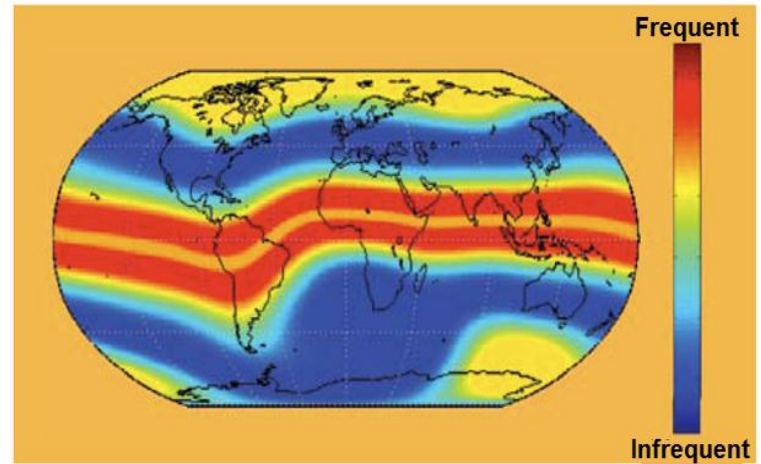
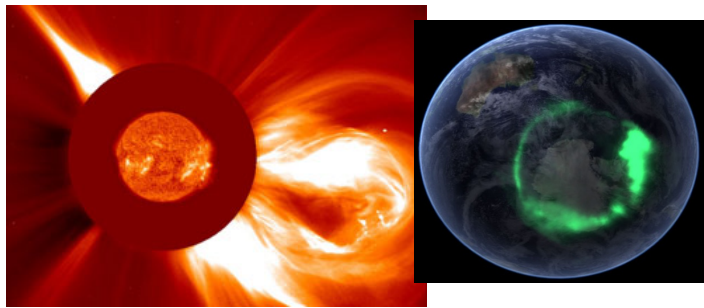
GPS Receiver Performance



Receiver Acquisition and Tracking



Ionospheric Scintillation Impact



GPS signals weak and GPS receiver loses observations and navigation capabilities

GPS Positioning Accuracy



Low

(single frequency,
metre-level accuracy)

High

(multiple frequencies,
centimetre-level accuracy)

GPS Positioning Accuracy

Affected by scintillation



Low

(single frequency,
metre-level accuracy)

High

(multiple frequencies,
centimetre-level accuracy)

What GNSS Needs

- Alarmist media statements? No
- Space weather predictions? Not really...
- Specification of structures, irregularities and gradients in electron density (ISR)
- Simulation tools for
 - assessing space weather impact on GPS modernization, Galileo and COMPASS
 - designs of future systems and signals

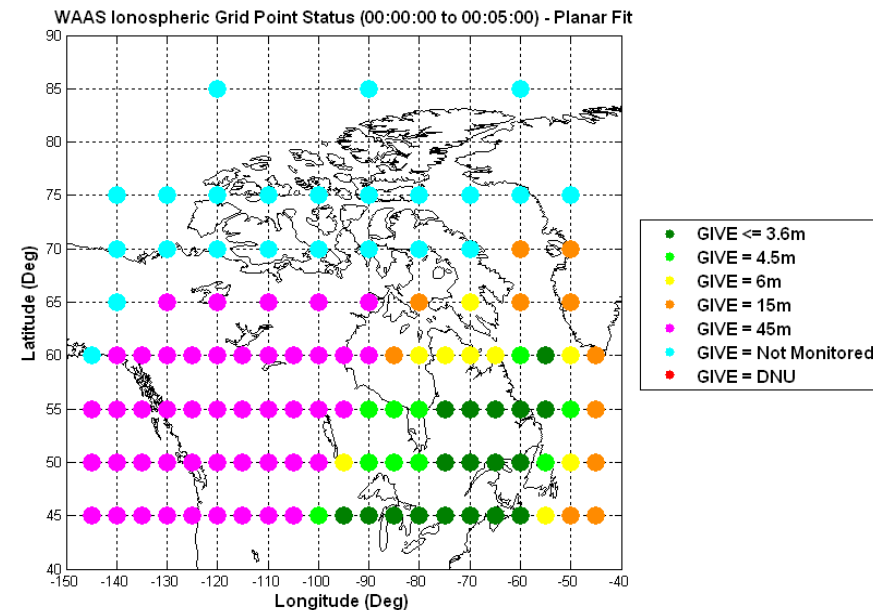
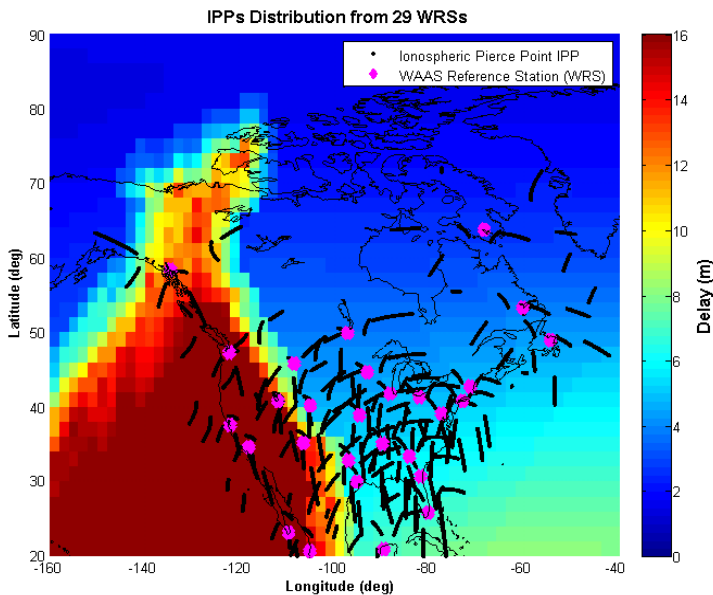
Project: Commercial Aviation

Sponsors/partners:

NAV CANADA, NASA/JPL

Objective:

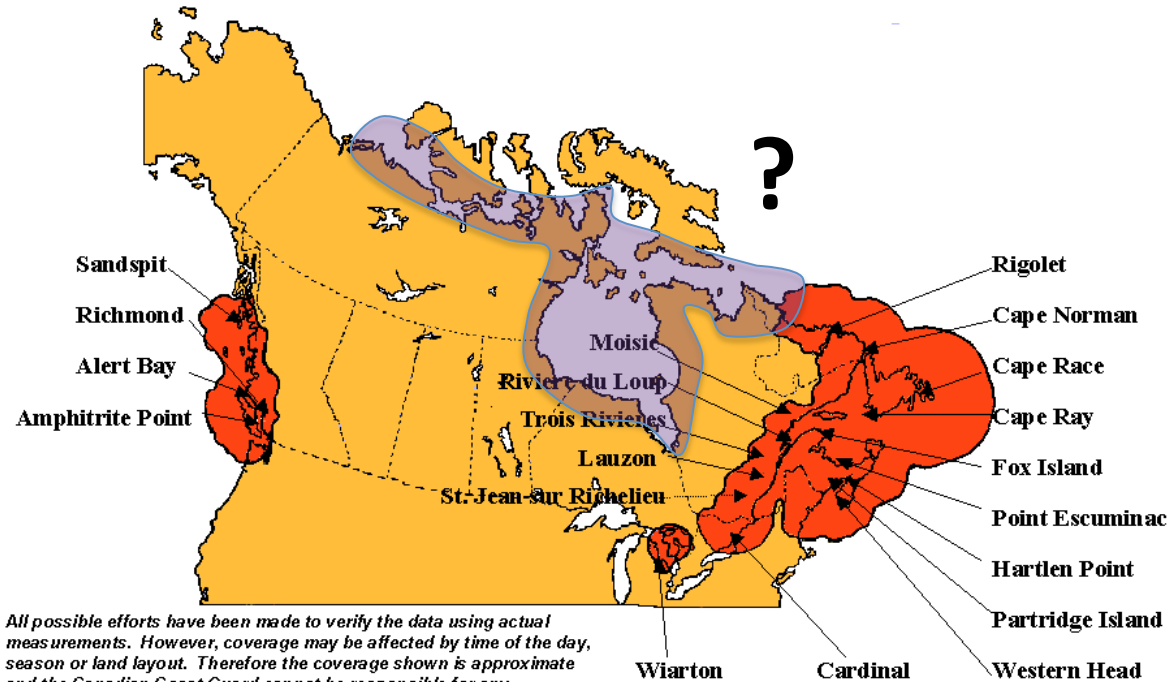
Detect and reduce space weather effects



Project: Maritime Navigation

Sponsors/partners:
Canadian Coast Guard

Objective:
Expand marine DGPS services
in northern Canada



All possible efforts have been made to verify the data using actual measurements. However, coverage may be affected by time of the day, season or land layout. Therefore the coverage shown is approximate and the Canadian Coast Guard cannot be responsible for any inaccuracies..

Project: Arctic Testbed

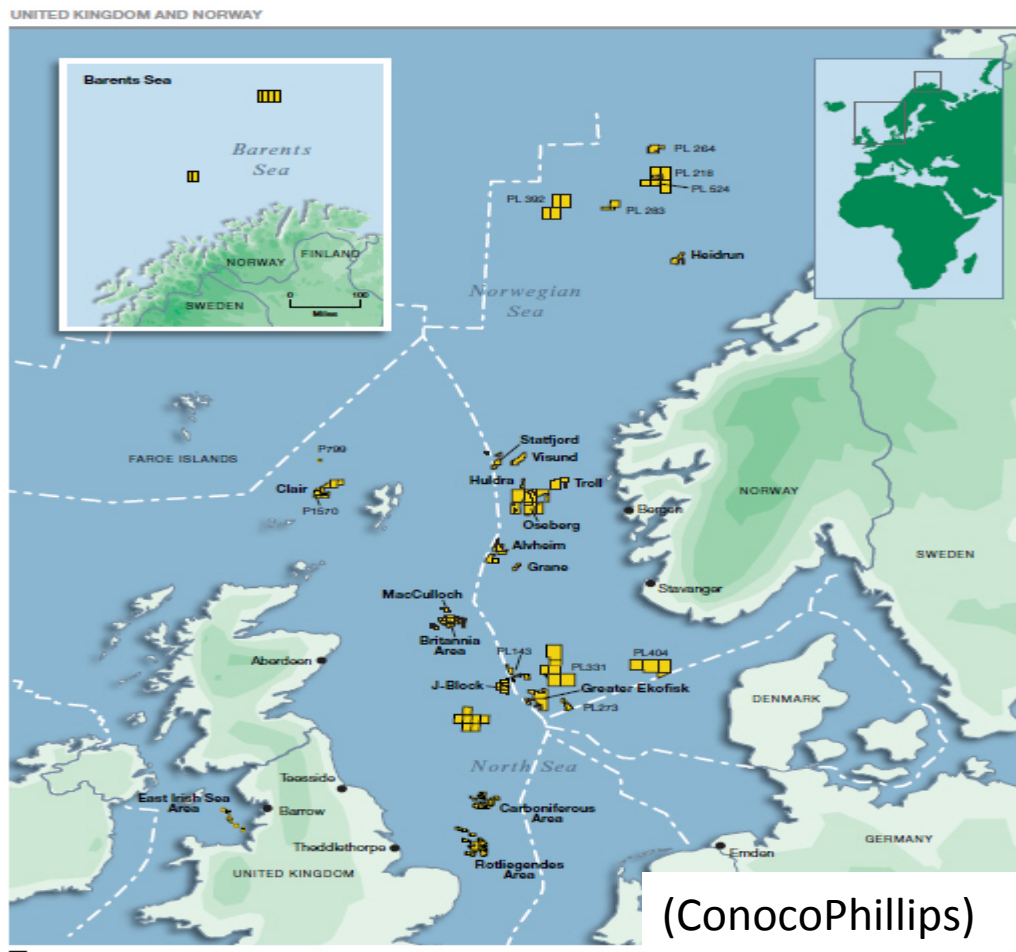
Sponsors/partners:

European Space Agency,
Kongsberg Seatex

Objective:

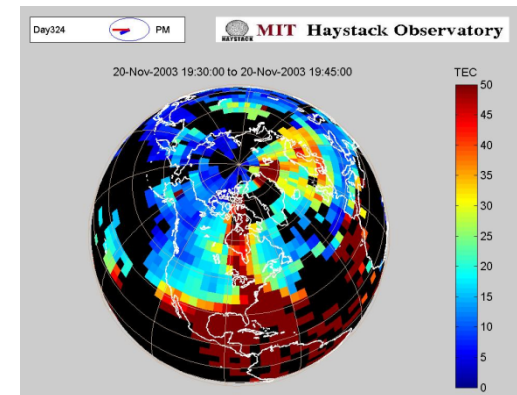
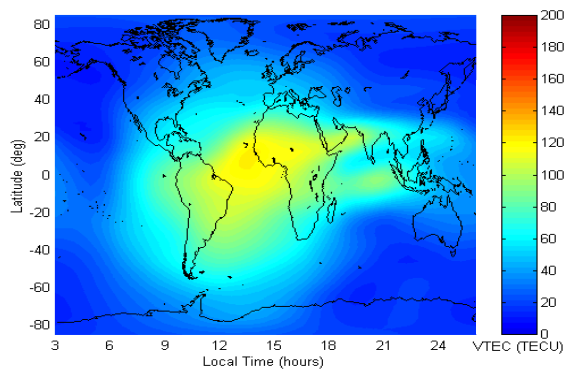
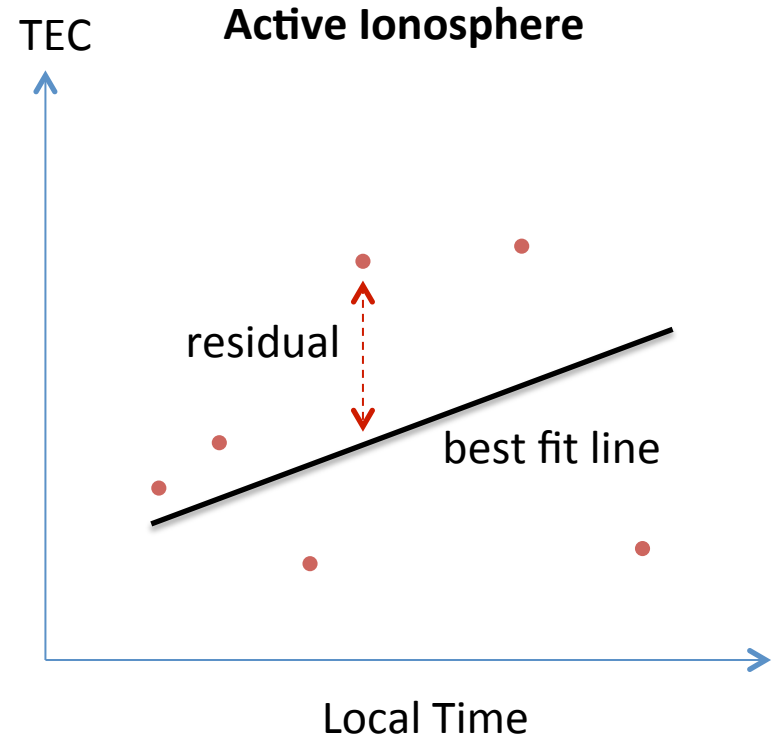
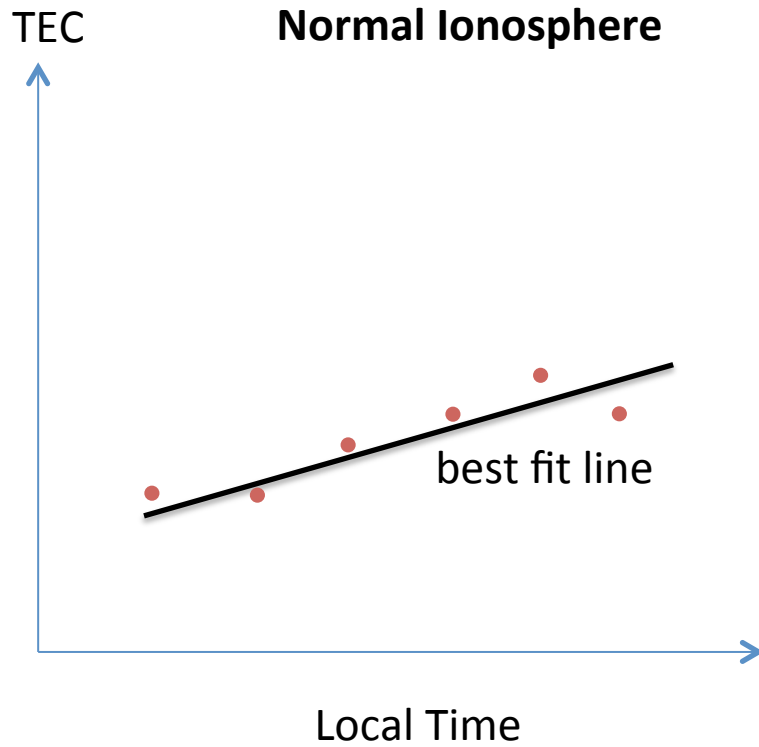
Determine optimal marine and aviation navigation services in European Arctic region

- Develop better navigation methods
- Develop improved GNSS receivers
- Develop space weather warnings

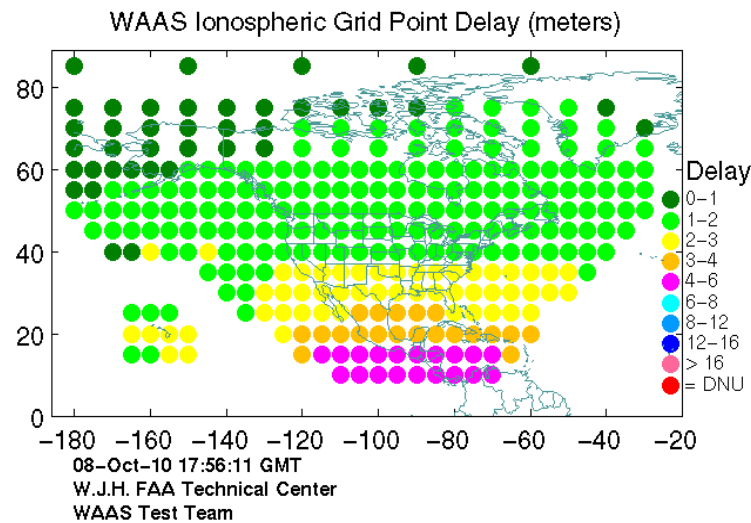
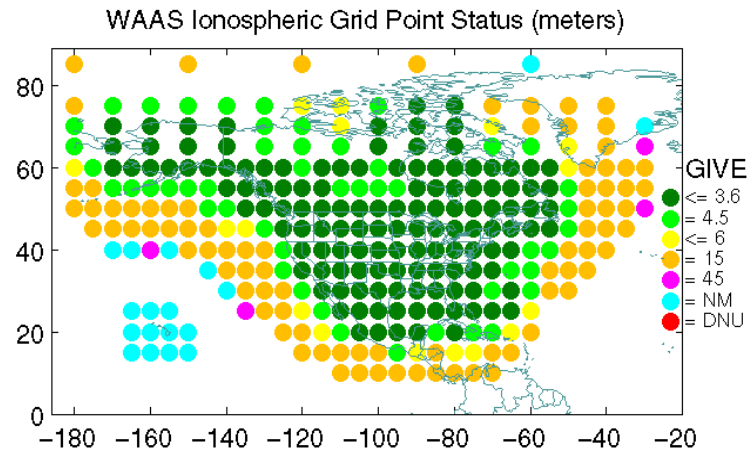


Extra

Error Bounds



WAAS Error Bounds



[http://www.nstb.tc.faa.gov/RT_WaasSIGPStatus.htm]